A Computational Model Integrating Electrophysiology, Contraction, and Mitochondrial Bioenergetics in the Ventricular Myocyte

Sonia Cortassa, Miguel A. Aon, Brian O'Rourke, Robert Jacques, Hsiang-Jer Tseng, Eduardo Marbán, and Raimond L. Winslow

The Johns Hopkins University, Institute for Computational Medicine, and Institute of Molecular Cardiobiology, Baltimore, Maryland

ABSTRACT An intricate network of reactions is involved in matching energy supply with demand in the heart. This complexity arises because energy production both modulates and is modulated by the electrophysiological and contractile activity of the cardiac myocyte. Here, we present an integrated mathematical model of the cardiac cell that links excitation-contraction coupling with mitochondrial energy generation. The dynamics of the model are described by a system of 50 ordinary differential equations. The formulation explicitly incorporates cytoplasmic ATP-consuming processes associated with force generation and ion transport, as well as the creatine kinase reaction. Changes in the electrical and contractile activity of the myocyte are coupled to mitochondrial energetics through the ATP, Ca²⁺, and Na⁺ concentrations in the myoplasmic and mitochondrial matrix compartments. The pseudo steady-state relationship between force and oxygen consumption at various stimulus frequencies and external Ca²⁺ concentrations is reproduced in both model simulations and direct experiments in cardiac trabeculae under normoxic conditions, recapitulating the linearity between cardiac work and respiration in the heart. Importantly, the model can also reproduce the rapid time-dependent changes in mitochondrial NADH and Ca²⁺ in response to abrupt changes in workload. The steady-state and dynamic responses of the model were conferred by ADP-dependent stimulation of mitochondrial oxidative phosphorylation and Ca²⁺-dependent regulation of Krebs cycle dehydrogenases, illustrating how the model can be used as a tool for investigating mechanisms underlying metabolic control in the heart.

INTRODUCTION

Control mechanisms that modulate mitochondrial ATP production to match energy consumption are especially important in tissues with a high energetic demand like the heart (1). The proportionality between cardiac work and the rate of respiration was recognized almost 100 years ago (2), yet the mechanisms responsible for matching energy supply with demand remain controversial (3). The metabolic rate can change by 10- to 15-fold (4,5), but many investigators have observed that the levels of energy-rich adenine intermediates can be remarkably constant, indicating that oxidative phosphorylation is tightly controlled (for review, see (6,7)).

Several hypotheses have been put forward to explain the control of oxidative phosphorylation. The classical respiratory control hypothesis of Chance and co-workers (8), which has been subsequently confirmed in countless experiments on isolated mitochondria, implies that the rate of respiration is limited by the availability of ADP to the mitochondrial ATP synthase (as long as adequate substrates are available to maintain proton pumping). This demand-led control would be well suited to increase ATP production in response to cytoplasmic ATP consumption, but changes in bulk cytoplasmic ADP concentration have not been detected in intact hearts at high workloads by phosphorous NMR methods. Furthermore, a large increase in total ADP would have an unfavorable effect

on cell processes that are sensitive to the free energy of ATP hydrolysis (i.e., the phosphorylation potential).

To explain how mitochondrial ADP delivery is accelerated without a large change in the cytoplasmic levels, models of intracellular dynamic compartmentation of adenine nucleotides have been proposed. This hypothesis is based on abundant evidence that different creatine kinase isozymes are localized near the sites of ATP hydrolysis (e.g., the myofibrils) and the mitochondrial inner membrane, contributing to intracellular-energetic units (9). This view implies that, whereas bulk ATP/ADP ratios remain constant, ADP signals generated by the myosin ATPase are rapidly transferred to the mitochondria via the creatine kinase shuttle. ATP can be similarly channeled back to the sites of utilization with alterations in the ATP/ADP ratio occurring only in microdomains close to the relevant sources and sinks of ATP (10). Evidence for compartmentalization of the adenine nucleotide pool has been addressed recently by combining biochemical models of phosphoryl transfer with estimations of CK fluxes by saturation transfer NMR methods (11).

Any mechanism that increases the rate of NADH oxidation would require concomitant activation of NADH production. Balaban and co-workers have proposed several mechanisms by which simultaneous stimulation of work and metabolism might be coordinated by cytoplasmic messengers. These include parallel activation of the respiratory chain and mitochondrial dehydrogenases by either Ca^{2^+} (12) or P_i (1,13). As elaborated in these studies, very rapid responses in the NADH production and oxidation processes would virtually eliminate transients in metabolite levels during changes in work.

Submitted October 14, 2005, and accepted for publication April 24, 2006. Address reprint requests to Raimond L. Winslow, The Johns Hopkins University, School of Medicine, Rm. 201B Clark Hall, 3400 N. Charles St., Baltimore MD 21218. Tel.: 410-516-5417; E-mail: rwinslow@jhu.edu.

To gain a better understanding of the complex dynamics of the response of mitochondrial bioenergetics to alterations in the contractile and electrical activity of the heart cell, and to explore the feasibility of proposed control mechanisms, here we integrate models of the electrophysiological, Ca²⁺ handling, and force-generation subsystems of the cardiac myocyte (14,15) with a model of mitochondrial oxidative phosphorylation (16). The model is validated by performing parallel experiments measuring force and oxygen consumption in cardiac trabeculae and by comparison with earlier data describing transients in NADH and mitochondrial Ca²⁺ during abrupt perturbations of muscle workload (17).

MATHEMATICAL MODEL DEVELOPMENT Excitation-contraction coupling/mitochondrial energetics (ECME) model

Fig. 1 shows the integrated model. The scheme emphasizes the links among mitochondrial metabolism, electrophysiology, and contraction.

Energy intermediates as links between mitochondrial energetics and excitation-contraction coupling

The excitation-contraction (EC) coupling (guinea-pig ventricular myocyte) and mitochondrial energetic models (14,15) are linked by the concentrations of ATP, ADP, creatine and creatine phosphate, and mitochondrial and cytoplasmic Ca^{2+} and Na^+ .

As discussed above, the currently accepted view that CK functions as both a cellular energy buffer and a high-energy phosphate shuttle (11,18,19) required us to introduce into the model a mechanism to simulate both the rapid transmission of an ADP signal to the mitochondria from the myo-filaments and the buffering of the bulk cytoplasmic ATP/ADP ratio by the creatine kinase (CK) system. To avoid the computational challenge of incorporating a spatial dimension and partial differential equations into the model, we approximated metabolic compartmentation by adding two pools of CK, creatine, and adenine nucleotides in the cytoplasm (Fig. 1). One pool is associated with mitochondrial transport through the adenine nucleotide translocator (ANT) and is linked to the EC coupling processes. The other pool accounts for energy provision to constitutive cytoplasmic processes, e.g. transport processes and macromolecule synthesis. In our model, adenine nucleotide levels provide a strong link between mitochondrial energetics and the electrophysiological and contractile processes (see Discussion).

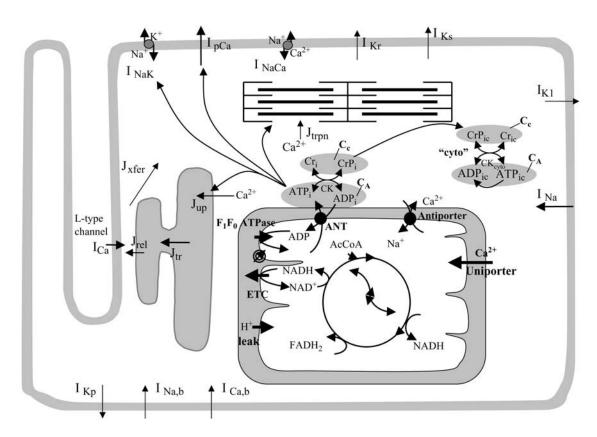


FIGURE 1 General scheme of the EC coupling/mitochondrial energetics (ECME) model. The electrophysiological module includes the main ion transport processes involved in EC-coupling, accounting for the transport of Ca^{2+} , Na^+ , and K^+ across the sarcolemma, Ca^{2+} transport inside and across the SR membrane, and Ca^{2+} handling by mitochondria. Five different Ca^{2+} compartments are defined including the mitochondrial matrix, the dyadic subspace, the junctional and network SR, and the myoplasmic compartments. Extracellular Ca^{2+} is considered an adjustable parameter. The mitochondrial module describes the production (F_1 , F_0 ATPase) and transport (ANT) of ATP, Ca^{2+} transport, and Ca^{2+} activation of the TCA cycle dehydrogenases. The CK reaction occurs near the mitochondria (but does not include potential limitations imposed by the outer membrane) and the CrP diffuses to the cytoplasmic compartment where there is another pool of CK that catalyzes the regeneration of ATP_{ic} to fuel constitutive cytoplasmic ATPases (labeled "cyto"). Also the total pool of adenine (C_A) and creatine (C_C) metabolites are indicated by dark shading. The main ATP-consuming processes related to EC coupling are the myofibrillar ATPase (V_{AM}) and SERCA (V_{up}), and in the sarcolemma, the V_{up} in the Sarcolemma, the V_{up} is a transport of the EC coupling are the myofibrillar ATPase (V_{AM}) and SERCA (V_{up}) and in the sarcolemma, the V_{up} is a transport of the EC coupling are the myofibrillar ATPase (V_{up}).

Our model also defines two different pools of ATP in the cytoplasm: ATP_i (EC coupling-linked) and ATP_{ic} (associated with constitutive cytoplasmic ATPases) (see Eqs. 1–5). In each one of these pools the total concentration of adenine nucleotides is constant, and the total concentration of adenine nucleotide, C_A , is the same (8 mM). Thus, the following equations apply:

$$[ADP]_{i} = C_{A} - [ATP]_{i}, \tag{1}$$

$$[ADP]_{ic} = C_A - [ATP]_{ic}. \tag{2}$$

This approach implies that ADP levels are determined by ATP in each cytoplasmic pool, linked through the creatine metabolites that are exchanged with the adenine metabolites by the CK catalyzed reaction:

$$ATP + Cr \stackrel{CK}{\rightleftharpoons} ADP + CrP$$

The rate of CK was modeled using mass action kinetics assuming that it operates close to thermodynamic equilibrium:

$$V_{\rm CK} = k_{\rm CK}^{\rm F} \left([\rm ATP][\rm Cr] - \frac{[\rm ADP][\rm CrP]}{K_{\rm FO}} \right). \tag{3}$$

Creatine phosphate (CrP) is synthesized from ATP by the mitochondrial CK ($V_{\rm CK}^{\rm mito}$) (Eq. A141) and transported to the cytoplasm for its utilization by constitutive energy-consuming processes through $V_{\rm C}^{\rm CrP}$ (Eq. A142). The CK at the cytoplasmic site, $V_{\rm CK}^{\rm cyto}$ (Eq. A140), catalyzes the phosphorylation of ADP from CrP to generate ATP (CK reaction as written above in the reverse direction) that will be used by the constitutive cytosolic ATPases ruled by $V_{\rm ATPase}^{\rm cyto}$ (fixed parameter, Table 12). Thus, the direction of the CK reaction depends on the enzyme localization, i.e., toward CrP synthesis in the mitochondria and toward the synthesis of ATP in the cytoplasm. The creatine metabolite levels in each pool, like the adenine nucleotide concentrations, are linked through conservation relationships as follows:

$$[Cr]_{i} = C_{c} - [CrP]_{i}, \tag{4}$$

$$[Cr]_{ic} = C_c - [CrP]_{ic}. \tag{5}$$

Equations 4 and 5 indicate that the Cr levels in both cytoplasmic pools are determined by the level of CrP. The parameter Cc (the total concentration of creatine metabolites) is the same in both pools, 25 mM (Table 12).

Ionic linkages between mitochondrial energetics and EC coupling

In addition to the ATP and ADP links between mitochondrial and cytoplasmic compartments, the mitochondrial concentration of Ca^{2+} ($[Ca^{2+}]_m$) is related to the myoplasmic Ca^{2+} concentration through the activity of the Ca^{2+} uniporter and the mitochondrial Na^+/Ca^{2+} exchanger (NCE). The NCE senses the cytoplasmic Na^+ level that is exchanged with Ca_m^{2+} . Thus, mitochondria act as an additional Ca^{2+} and Na^+ sink in our model.

The rate expressions accounting for the dynamics of the ATP-consuming processes in the cytoplasm have been modified to account for their dependence on ATP and ADP concentrations. Among those energy-dependent processes are: the sarcoplasmic reticulum Ca²⁺ pump (SERCA); the Na⁺/K⁺ ATPase; and the sarcolemmal Ca²⁺ pump. The ATP-dependence of the kinetics of these pumps is detailed in the following sections.

Cytoplasmic ATP-consuming processes

Sarcoplasmic-endoplasmic reticulum Ca²⁺ ATPase (SERCA)

Rice and collaborators (15) adopted the Shannon et al. (20) formulation of SERCA kinetics. This equation (Eq. 6) incorporates the forward and reverse modes of Ca^{2+} transport across the sarcoplasmic reticulum (SR) membrane.

We modified the original rate expression to account for ATP-dependence of SERCA, in accordance with experimental data obtained in vitro by Sakamoto and Tonomura (21) using a fragmented SR preparation. These studies demonstrated a Michaelis-Menten dependence of enzyme activity with respect to ATP and mixed-type inhibition of the enzyme by ADP under conditions of high Mg²⁺ and low Ca²⁺. The experimental data (21) were also incorporated by Jeneson et al. (22) in their model of energy cycling in human skeletal muscle. Equation 6 represents the rate of the SERCA, explicitly describing its ATP and ADP dependence. The factor that incorporates [ATP]_{ii} and [ADP]_i in the denominator has been adopted from Jeneson et al. (22) with the parameter values determined by Sakamoto and Tonomura (21),

$$V_{\text{SERCA}} = \frac{K_{\text{SR}}[V_{\text{maxf}}f_{\text{b}} - V_{\text{maxr}}r_{\text{b}}]}{1 + f_{\text{b}} + r_{\text{b}}} \times \frac{1}{\frac{K_{\text{m,up}}^{\text{ATP}}}{[\text{ATP}]_{\text{i}}} \left(1 + \frac{[\text{ADP}]_{\text{i}}}{K_{\text{i,up}}}\right) + \left[1 + \frac{[\text{ADP}]_{\text{i}}}{K'_{\text{i,up}}}\right]}, \quad (6)$$

being

$$f_{\mathrm{b}} = \left(\frac{\left[\mathrm{Ca}^{2^{+}}\right]_{\mathrm{i}}}{K_{\mathrm{fb}}}\right)^{\mathrm{Nfb}},$$

and

$$r_{\rm b} = \left(\frac{\left[{\rm Ca}^{2^+}\right]_{\rm NSR}}{K_{\rm rb}}\right)^{\rm Nrb},$$

where $K_{\rm m}^{\rm ATP}$ represents the affinity of SERCA for ATP, and $K_{\rm i,up}$ and $K'_{\rm i,up}$ are the ADP inhibition constants (Table 7). As shown experimentally by Sakamoto and Tonomura (21), Eq. 6 indicates that ADP inhibits the pump both by competitive (accomplished in the term containing $K_{\rm i,up}$) and noncompetitive (accounted for by $K'_{\rm i,up}$) mechanisms. We simulated the behavior of SERCA as a function of ${\rm Ca}^{2+}$ concentrations in the myoplasm and inside the SR network (NSR). The introduction of ATP dependence did not significantly change pump rate as a function of ${\rm Ca}^{2+}$ in the physiological range of ATP_i levels (not shown).

Actomyosin ATPase (AM ATPase)

The data of Regnier et al. (23), concerning mechanisms involved in the regulation of force generation by cardiac muscle, indicate little sensitivity of developed muscle tension to large variations in ATP (from 0.5 to 5 mM). Additionally, Karatzaferi et al. (24) demonstrated that ADP analogs bind to myosin heads, thereby potentiating tension. Accordingly, we assume that developed force is only indirectly sensitive to the ratio of ATP to ADP (see Eqs A96–A121) through the effect of the latter on the SERCA pump, resulting in reduced sarcoplasmic reticulum Ca²⁺ load leading to reduced developed force. On the other hand, the rate of ATP hydrolysis associated with force generation through actomyosin ATPase (Eq. 7) depends explicitly on both ATP and ADP, as previously demonstrated (25). We have developed a Michaelis-Menten kinetic expression to account for ATP activation of the actomyosin ATPase associated with force generation, together with a competitive ADP inhibition:

$$V_{\text{AM}} = V_{\text{AM}}^{\text{max}} \left(\frac{f_{01}[P_0] + f_{12}[P_1] + f_{23}[P_2]}{f_{01} + f_{12} + f_{23}} \right) \times \frac{1}{1 + \frac{K_{\text{M,AM}}^{\text{ATP}}}{[\text{ATP}]_i}} \left[1 + \frac{[\text{ADP}]_i}{K_{i,\text{AM}}} \right].$$
(7)

Equation 7 contains a factor accounting for dependence of the AM ATPase on normalized rate of cross-bridge formation through their rate of formation,

as denoted by f_{01} [P₀], f_{12} [P₁, and f_{23} [P₂] and the rate constants f_{01} , f_{12} , and f_{23} (Eqs. A102–A104).

Na⁺/K⁺ ATPase

The original expression for the $\mathrm{Na}^+/\mathrm{K}^+$ ATPase corresponds to that introduced by Luo and Rudy in their phase II ventricular cell model (26). This model was able to account for experimental observations performed by Nakao and Gadsby (27) regarding the dependence of the current on membrane potential at different external Na^+ concentrations. The $\mathrm{Na}^+/\mathrm{K}^+$ current expression has been modified based on kinetic studies of Sakamoto and Tonomura (21) to account for the dependence of $\mathrm{Na}^+/\mathrm{K}^+$ ATPase activity on ATP, as well as the competitive inhibition exerted by ADP,

$$I_{\text{NaK}} = I_{\text{NaK,max}} f_{\text{NaK}} \frac{1}{\left[1 + \frac{K_{\text{m,NaK}}^{\text{ATP}}}{\left[\text{ATP}\right]_{i}} \left(1 + \frac{\left[\text{ADP}\right]_{i}}{K_{i,\text{NaK}}^{\text{ADP}}}\right)\right]} \times \frac{\frac{\left[\text{K}^{+}\right]_{o}}{\left[\text{K}^{+}\right]_{o} + K_{\text{m,Ko}}}}{1 + \left(\frac{K_{\text{m,Nai}}}{\left[\text{Na}^{+}\right]_{i}}\right)^{3/2}},$$
(8)

being

$$f_{\text{NaK}} = \frac{1}{1 + 0.1245 e^{\left(-0.1\frac{\text{VE}}{\text{RT}}\right)} + 0.0365 \,\sigma \,e^{\left(-\frac{\text{VE}}{\text{RT}}\right)}},$$

with

$$\sigma = \frac{e^{\left(\frac{\left[\operatorname{Na}^+\right]_o}{67.3}\right)} - 1}{7}.$$

Sarcolemmal Ca²⁺ ATPase

Equation 9 gives the modified rate expression incorporating the ATP-dependence of pump activity. Sarcolemmal $\operatorname{Ca^{2+}}$ ATPase rate (Eq. 9) exhibits two different $K_{0.5}$ values for ATP ($K_{\text{ml-pCa}}^{\text{ATP}}$, $K_{\text{m2-pCa}}^{\text{ATP}}$). ADP exerts competitive inhibition of the $\operatorname{Ca^{2+}}$ pump by affecting the high-affinity component of the ATP interaction through the inhibition constant, $K_{\text{i-pCa}}^{\text{ADP}}$. We adopted the $K_{0.5}$ values described in Echarte et al. (28), who found two $K_{0.5}$ values for ATP in their study of the enzyme reaction mechanism involving the formation of an intermediate phosphorylated enzyme state. The affinity constants for ATP suggested the presence of two nucleotide regulatory sites in the sarcolemmal $\operatorname{Ca^{2+}}$ ATPase (29):

$$I_{pCa} = I_{pCa_max} \left[\frac{1}{1 + \frac{K_{m1_pCa}^{ATP}}{[ATP]_{i}}} + \frac{1}{1 + \frac{K_{m2_pCa}^{ATP}}{[ATP]_{i}}} \right] \times \frac{[Ca^{2+}]_{i}}{K_{m}^{pCa} + [Ca^{2+}]_{i}}.$$
(9)

ATP/ADP dependence of the kinetics of the pumps

Fig. 2 displays the behavior of the different pumps introduced in the previous sections as a function of [ATP]_i. To compare the modeling results to

experimental data obtained in vitro, the simulations employed in vitro $V_{\rm max}$ values. These differed from the $V_{\rm max}$ values used in the integrated cell model because adjustments were required to simulate the reported currents or fluxes measured in intact cardiac myocytes.

The experimental results describing the behavior of the sarcoplasmic reticulum Ca^{2+} pump (Fig. 2 A) (from (21)) were simulated using the rate expression (Eq. 6) depicted in Fig. 2 B for the range of ADP concentrations employed by Sakamoto and Tonomura (21). Only the forward and reverse V_{max} values had to be adjusted in the model (see Table 7) to reproduce the SERCA pump fluxes obtained experimentally (20).

The dependence of the AM ATPase rate on ATP, measured by Karatzaferi et al. (24) (Fig. 2 C), could be reproduced using the rate expression of Eq. 7 (Fig. 2 D). As a result of the high affinity of the ATPase for the nucleotide, the rate of ATP consumption by myofibrils will be saturated with ATP in the physiological concentration range (not shown).

Fig. 2 E shows the current carried by the Na $^+$ /K $^+$ ATPase, measured experimentally by Sakamoto and Tonomura (21), and simulated using the rate expression shown in Eq. 8 (Fig. 2 F). The expression displays a typical hyperbolic dependence on ATP $_i$ concentration that saturates at ATP > 4.0 mM.

The rate of the sarcolemmal Ca^{2+} pump studied as a function of ATP concentration also exhibits a hyperbolic shape with saturation at high ATP levels (Fig. 2, G and H). As in the case of the AM ATPase, and in the normal physiological range of adenine nucleotide levels, the flux through the sarcolemmal Ca^{2+} pump will be nearly ATP-independent.

The absolute rates of ATP consumption in the integrated model were calculated based on the absolute fluxes or currents sustained by the ATP-consuming processes multiplied by the stoichiometry of such processes, e.g., 1 ATP is hydrolyzed by SERCA when transporting one Ca²⁺ from the cytosolic into the sarcoplasmic reticulum compartment. The resulting fluxes of ATP consumption were compared with available experimental evidence by Ebus and Stienen (30) and validated by showing that simulated consumption fluxes were in the correct range.

Computational methods

Rate expressions for each individual model component have been analyzed for their kinetic properties as a module. We used MatLab 6.5 (The MathWorks, Natick, MA) to study each rate expression separately from the assembled model and to check for the adequacy of the rate law and the parameter set being used. Once the behavior of each rate function proved satisfactory, the code of the ECME model, written in C⁺⁺, was assembled as a system of 50 ordinary differential equations (ODEs) in the development environment of Microsoft Visual Studio (Microsoft, Redmond, WA). Equations were integrated numerically using CVODE, a stiff ODEs solver in C, developed by Cohen and Hindmarsh (31), that uses variable-coefficient Adams and BDF methods (http://citeseer.ist.psu.edu/1230.html).

Before starting to run any specific protocol, we simulated the behavior of the system without stimulation to reach a steady state. Subsequently, the model was run for \sim 800 s with pacing at 0.25 Hz. The state attained after 800 s is, in fact, a point in a steady trajectory of state variables. In such a trajectory it may be verified that most of the EC coupling related variables (e.g., V, $[Ca^{2+}]_i$, and the level of Ca^{2+} in the dyadic subspace: $[Ca^{2+}]_{SS}$) change periodically as a result of the periodic stimulus (illustrated in Supplementary Material, Fig. S1). Since the trajectories described by the variables are constant, this state will be described as a pseudo-steady state, which defined the initial condition for all runs in a series of experiments. The different protocols tested were programmed as a subroutine in the main file of the program code. Changes in the pacing frequency were programmed according to the experimental protocol of Brandes and Bers ((17,32); see their article, section called Time-Dependent Changes in Workload), but were entered manually for the pseudo-steady state studies of the force-frequency relations. During simulation, the results output is stored as text files that are analyzed later with the assistance of Microcal Origin 6.0 (Microcal Software, Northampton, MA).

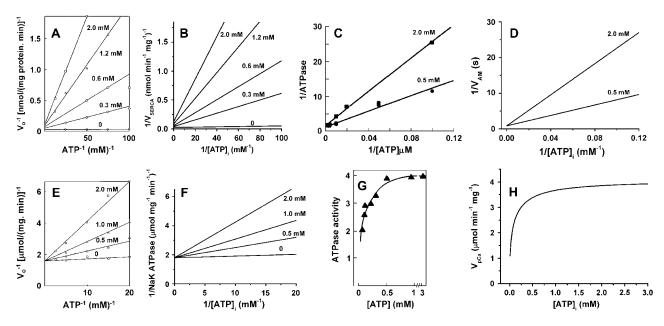


FIGURE 2 ATP/ADP dependence of cytoplasmic and sarcolemmal pumps. (A and B) The dependence of the SERCA flux (J_{up}) on cytoplasmic ATP. Panel A shows experimental data redrawn from Sakamoto and Tonomura (21) and panel B shows model simulations using the SERCA rate equation (Eq. 6). The curves labeled 0, 0.3, 0.6, 1.2, and 2.0 mM illustrate the inhibitory effect of increasing ADP concentration. The parameters were set to: $V_{max f} = 60 \text{ nmol mg}^{-1}$ protein \min^{-1} ; $V_{max r} = 64 \text{ nmol mg}^{-1}$ protein \min^{-1} ; $Ca^{2+}]_i = 0.5 \text{ mM}$; and $Ca^{2+}]_{NSR} = 0.3 \text{ mM}$. All the other parameters are as indicated in Table 7. (C and D) The dependence of the myofibrillar adenosine triphosphatase (V_{AM}) on cytoplasmic ATP. Panel C shows experimental data redrawn from Karatzaferi et al. (24) and panel D shows model simulations obtained with Eq. 7 (also Eq. A122). The competitive inhibition by ADP is shown for ADP concentrations of 0.5 and 2.0 mM ADP. The plots were produced with a maximal rate of the myofibrillar ATPase, V_{MA}^{mx} , of 2.88 s⁻¹, and $P_1 = 0.2$, $P_2 = 0.7$, and $P_3 = 0.1$. Otherwise, the parameters used in the plot are as indicated in Table 11. (E and F) The dependence of the Na⁺, K⁺ adenosine triphosphatase activity on ATP. Experimental data (E, from (21)) and model simulations (F) using the rate expression of Eq. 8. Competitive inhibition by ADP at 0, 0.5, 1.0, and 2.0 mM concentrations is shown. The parameters used were $V_{max} = 3.93 \text{ } \mu \text{mol mg}^{-1} \text{ min}^{-1}$, the membrane potential is -80 mV, and the intracellular Na⁺ is 7.0 mM. The other parameters are as indicated in Table 3. (G and H) The dependence of the sarcolemmal Ca^{2+} adenosine triphosphatase activity on ATP. Experimental data (G, from (29)) and model simulations (H) obtained with Eq. 9, which corresponds to a typical Michaelis-Menten profile. The following parameter values were used in the simulation: $V_{max} = 2.55 \mu \text{mol mg}^{-1} \min^{-1}$; V_{m

Experimental methods

Muscle preparation and experimental setup

Male LBN-F1 rats weighing 175-250 g (Harlan Sprague Dawley; Indianapolis, IN) were anesthetized by intraperitoneal injection of 1.0 ml/kg pentobarbital sodium (360 mg/ml). After intracardiac heparinization, the hearts were rapidly excised and placed in Krebs-Henseleit buffer containing (in mM): 120 NaCl, 5 KCl, 2 MgSO₄, 1.2 NaH₂PO₄, 20 NaHCO₃, 0.25 Ca²⁺, and 10 glucose (pH 7.4). Additionally, 20 mM 2,3-butanedione monoxime (BDM) was added to the dissection buffer to prevent cutting injury. The effects of BDM after brief exposure have been found to be reversible (33). Hearts were cannulated via the ascending aorta and retrogradely perfused with the same buffer equilibrated with 95% O₂–5% CO₂. A flat, uniform, unbranched trabecula from the right ventricle was carefully dissected, leaving a block of tissue at one end from the right ventricle free wall and a small part of the valve at the other end to facilitate mounting. The dimensions of the muscles were measured using a calibration reticle in the ocular of the dissection microscope. The muscles have an oval cross-sectional profile with an average width of 0.29 \pm 0.05 mm and a thickness of 0.097 \pm 0.028 mm. This small muscle dimension assures an adequate supply of oxygen to the whole tissue volume. The cross-sectional area, calculated assuming an ellipsoid shape, averaged 0.022 mm². All experimental protocols conformed to Johns Hopkins University institutional guidelines regarding the use and care of animals.

Trabeculae were mounted between a basket-shaped extension of the force transducer and a hooklike extension of a micromanipulator screw with the aid of a dissection microscope. This attachment and mounting procedure was chosen because it proved to minimize damage to the muscle preparation (34). The muscles were stretched until a further increase in length would cause the resting and developed tensions to increase in parallel, corresponding to a sarcomere length (2.2 μ m) that is slightly below the maximal developed tension (34).

To monitor the contractile parameters during the experiment, each twitch was analyzed on-line with a subroutine developed for LabVIEW (Ver. 6.1, National Instruments, Austin, TX) that acquires and processes the raw data from the force transducer. The forces developed by the rat trabeculae were computed in mN.mm⁻². These were displayed as relative changes in force to compare them with the simulations, since the model was based on guineapig EC coupling properties, which produces different absolute tensions.

Respiration measurements

We used a fiber-optic oxygen sensor (Ocean Optics, Dunedin, FL) to measure muscle respiration. This probe works as a spectrometer-coupled chemical sensor for full spectral analysis of dissolved oxygen pressure. The principle of detection is the fluorescence emission at 600 nm of a ruthenium compound that is quenched by O_2 . At the tip of the fiber optic probe ($\emptyset = 300 \, \mu m$), the O_2 -sensitive compound is embedded in a resin. The fluorescence emitted is a function of the O_2 dissolved in the surroundings of the probe.

The respiratory flux was measured with the fiber-optic device monitoring the O_2 levels close to the surface of contracting trabeculae (within 200 μ m) upon interruption of the perfusion flow during a 45-s to 1-min interval.

Under these conditions, we recorded a linear change in the fluorescent signal whose slope is proportional to the respiratory flux. As expected, the respiratory rate increases with the frequency of stimulation and the ${\rm Ca}^{2^+}$ levels in the buffer bathing the muscle. The measurements were referred to the maximal levels of respiration attained under the experimental conditions described in the presence of the uncoupler FCCP (1 μ M). The respiratory flux was completely inhibited in the presence of NaCN (5 mM). All our experimental recordings were performed at 22°C.

RESULTS

Force-frequency relations

Fundamental cardiac muscle properties were explored by examining the energetic and inotropic responses to an increase in stimulation frequency. This force-frequency relation is muscle type- (atrial or ventricular) and species-specific (35,36). The force-frequency relation has been studied under pseudo steady-state and transient conditions (see next section).

Pseudo steady-state studies

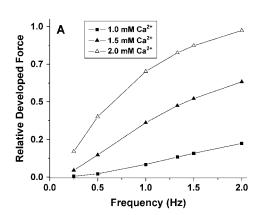
The force versus frequency studies under pseudo-steady state in silico conditions were performed by varying the frequency of pacing and analyzing the model behavior after $\sim 500-1000 \, \mathrm{s}$ (8–15 min) of simulation time at each frequency.

Systolic (maximal) and diastolic (minimal) forces were computed from the behavior during one beat immediately after 800 s of simulation under each parametric condition. Developed force was computed as the difference between the systolic and the diastolic force. Fig. 3 A shows dependence of developed force as a function of frequency at three different levels of extracellular Ca²⁺, [Ca²⁺]_o. In the range of [Ca²⁺]_o studied, force increased linearly with frequency, attaining a value of 32 mN mm⁻² at 2.0 Hz in 2.0 mM Ca²⁺. The slope of the force-frequency relationship increased with increased [Ca²⁺]_o. The increment in developed tension correlates with the increase in the amplitude of the Ca²⁺ transient in the cytosol (see Supplementary Material, Fig. S2). This ''positive staircase'' results from enhanced time-averaged

 ${\rm Ca}^{2+}$ entry and SR ${\rm Ca}^{2+}$ loading and is, in part, indirectly influenced by intracellular ${\rm Na}^+$ concentration, which modulates SR ${\rm Ca}^{2+}$ load by shifting the balance of ${\rm Ca}^{2+}$ fluxes through the actions of the sarcolemmal ${\rm Na}^+/{\rm Ca}^{2+}$ exchanger.

Simulated force-frequency relations (Fig. 3 *A*) qualitatively resembled those obtained experimentally in the cardiac rat trabeculae (Fig. 3 *B*). However, quantitative differences were found between experimental data and model predictions, especially for values obtained at low Ca²⁺ concentration. The slope of the force versus frequency relationship at 1.0 mM extracellular Ca²⁺ was much larger in the experiments than in the model (Fig. 3). In the simulations, force values changed by 30-fold when stimulation frequency increased from 0.25 to 2.0 Hz, whereas in rat trabeculae, force increased only approximately threefold in the presence of 1.0 mM extracellular Ca²⁺ between 0.25 and 2 Hz.

The bioenergetic performance of the system, monitored through the rate of oxygen consumption (V_{O2}) , was also studied using the same experimental setup for isometric force measurements in rat ventricular trabeculae (see Experimental Methods). In this way, we could not only directly compare experimental contractile activity with in silico data but also measure $V_{\rm O2}$ as a function of the pacing frequency. The value $V_{\rm O2}$ increased with the frequency of stimulation in the model under pseudo steady-state conditions, depending on [Ca²⁺]_o (Fig. 4 A). At high $[Ca^{2+}]_0$, the frequency- V_{O2} relationship displays a close to linear dependence, which was also reflected in simulations of the NADH levels (not shown). In the model, an increase in frequency will increase the levels of cytosolic Ca²⁺ and ADP, which will be translated into higher mitochondrial $[Ca^{2+}]_m$ and $[ADP]_m$ (not shown) to activate two main mechanisms for activating oxidative phosphorylation. [Ca²⁺]_m will stimulate the TCA cycle dehydrogenases, whereas [ADP]_m will activate respiration through respiratory control. The close-to-linear increase in respiration with frequency is likely due to a larger effect of the TCA dehydrogenases stimulation by Ca²⁺ than the corresponding ADP stimulation of respiration as also suggested by the NADH profile (not shown).



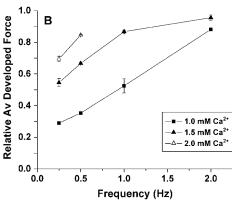
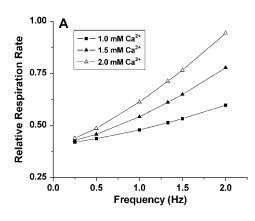


FIGURE 3 Force-frequency relations. Developed force simulated by the ECME model (A) and measured in experiments on rat ventricular trabeculae (B) as a function of the pacing frequency at various extracellular Ca²⁺ levels. The simulations were run for 1500 s from the initial condition indicated in Table 16. The parameters used are as described in Tables 1-15 except for the extracellular Ca²⁺ concentration, which is indicated in the legend. The developed force was calculated after the model reached a pseudo-steady state from the difference between the maximum and the minimum forces during a contraction. The experiment data point shown for 1.5 mM Ca²⁺ at 0.25 Hz corresponded to a developed tension of 45 mN mm⁻².



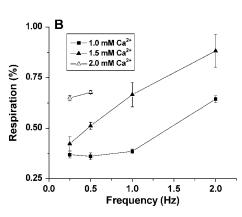


FIGURE 4 Respiration associated with force-frequency relations. O2 consumption simulated by the ECME model (A) and measured in rat ventricular trabeculae (B) as a function of the pacing frequency at various extracellular Ca²⁺ levels. The plots in panel A were obtained from the same simulations reported in Fig. 3. The experimentally determined rate of respiration, $V_{\rm O2}$, is expressed relative to the maximum observed when the muscle was exposed to the uncoupler FCCP. Treatment with 5 mM NaCN completely inhibited the respiratory flux. The simulated $V_{\rm O2}$ was averaged after the model reached a pseudo-steady state. Under steady-state resting conditions, $V_{\rm O2}$ averaged 0.08 mM s⁻¹.

Model simulations were qualitatively in line with the experimental data obtained in rat ventricular trabeculae (Fig. 4 *B*). Representing the combined data from Figs. 3 and 4 as the respiratory rate versus developed tension shows the proportionality between respiration and mechanical work that has been reported previously in working hearts (37) (see Supplementary Material, Fig. S3). The quantitative differences observed in Fig. 4 are, at least in part, due to the fact that the model has been designed and the parameters adjusted for the dynamics of guinea-pig ventricular myocytes, while the experimental system corresponds to rat ventricular trabeculae (see Discussion).

Time-dependent behavior of mitochondrial energetics after changes in workload

We explored the time-dependent behavior of the model with a protocol in which the stimulus frequency was raised from 0.25 to 2.0 Hz and then returned to 0.25 Hz. This protocol has been previously used experimentally in a preparation of ventricular rat trabeculae while mitochondrial energetic and EC coupling variables were monitored (17,32).

The increase in pacing frequency produces a drop in the level of NADH (undershoot, phase I in Fig. 5 A) followed by a recovery phase (phase II in Fig. 5 A) until a new steady NADH level is reached. A subsequent decrease in the pacing frequency causes an overshoot in the NADH concentration (phase III in Fig. 5 A), which is later followed by a relaxation toward the baseline NADH level. The ECME simulation of the same pacing protocol used by Brandes and Bers (17,32) qualitatively reproduces the profile of NADH and Ca_m^{2+} recorded experimentally (Fig. 5, A and B). The magnitude of the NADH decrease during the undershoot is somewhat lower than that observed experimentally (3% against 10%, respectively).

The ATP and CrP levels of the pool related to EC coupling during the transient is shown in Fig. 5 *C*. The decrease in ATP after the increase in pacing frequency is barely noticeable, because of the efficient buffering by CrP, whose levels

decrease ~3 mM. This result may be compared with the changes associated with an increase in heart rate in ferret hearts, whose phosphorylated energy intermediates were monitored over time with ³¹P NMR (38). Our simulations reproduce the profile in CrP when glycolysis is not operating. Moreover, the model behavior also simulates the lack of change in the total ATP observed during stimulation at 2 Hz (38).

Ca²⁺- and ADP-mediated regulatory mechanisms involved in mitochondrial energy supply

Once validated, an advantage of the integrated model is that it may be used to test competing hypotheses reported in the literature concerning the various mechanisms involved in the regulation of energy supply and demand in the heart. A similar approach was followed in the case of the isolated mitochondrial model (16).

Two basic control mechanisms are incorporated into the model, so it was essential to determine the independent contributions of each in the transient responses to the perturbation of workload. First, respiratory control by ATP consumption leading to increased ADP concentrations in both the cytoplasm and the mitochondrial matrix was eliminated by clamping cytosolic ATP and ADP to a constant levels. Second, the Ca²⁺-dependence of the activation of the Krebs cycle dehydrogenases was adjusted to abolish the upstream effect of Ca²⁺ to increase NADH production. This was accomplished by eliminating the effects of Ca²⁺ on the IDH and KGDH rates (Eqs. A147 and A149). Both tests were performed with the same parameter set and frequency range used in the control simulation shown in Fig. 5 A.

As shown in Fig. 6, when ATP_i is clamped, the dynamics of the simulated mitochondrial NADH signal are completely altered. Upon an increase in pacing frequency, there is no undershoot of the NADH signal and the NADH increases monotonically with a rate similar to that observed during the recovery phase of the transient in the earlier simulations

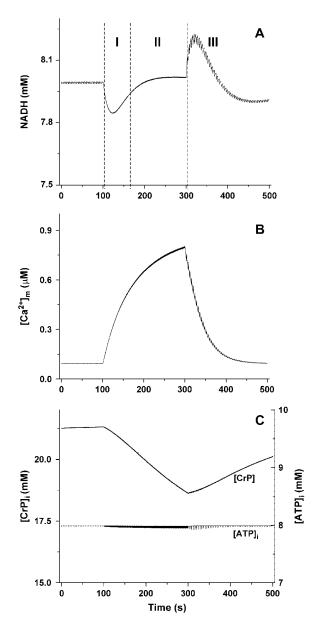


FIGURE 5 Mitochondrial energetics in response to changes in workload. Model simulations are shown for a change in the myocyte pacing frequency from $0.25 \, \text{Hz} (0-100 \, \text{s})$ to $2.0 \, \text{Hz} (100-300 \, \text{s})$ and back to $0.25 \, \text{Hz} (300-500 \, \text{s})$. The parameters and initial conditions used in the simulations are as indicated in Tables 1-16. The NADH time course (A) and mitochondrial matrix Ca^{2+} concentrations (B) are plotted. Regions I, II, and III indicate the different phases in the temporal evolution of the NADH signal. Panel C shows the profile of [ATP]_i and [CrP]_i obtained in the same simulation.

(phase *II*, Fig. 5 *A*). The NADH overshoot (phase *III*) is also eliminated when ATP_i is clamped (Fig. 6 *A*).

Removing Ca^{2+} -dependent activation of the dehydrogenases (Fig. 6 *B*) reveals the underlying effect of the stimulation of respiration by ADP. When pacing frequency is increased, the concentration of NADH drops to lower levels than in the control (compare phases *I*, in Figs. 5 *A* and 6 *B*) and does not recover (compare phases *II*, in Figs. 5 *A* and

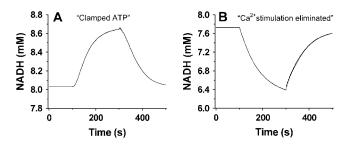


FIGURE 6 Contribution of Ca²⁺ activation of mitochondrial dehydrogenases and respiratory control by ADP to mitochondrial NADH dynamics. (A) The profile of NADH in simulations run with the pacing protocol indicated in Fig. 5, with myoplasmic ATP (both ATP_i and ATP_{ic}) clamped. (B) The NADH profile when the factor accounting for the stimulation by Ca²⁺ of IDH and KGDH is eliminated from the corresponding equations (see Eqs. A145 and A148).

6 *B*). Upon return to the low pacing frequency, NADH increases monotonically in time (Fig. 6 *B*).

These results illustrate how the interplay between ADPdependent stimulation of respiration and Ca²⁺-mediated activation of the Krebs cycle dehydrogenases accounts for the transient kinetics of the NADH response during changes in workload. Changes in force are rapidly manifested as changes in the NADH oxidation rate by respiration, leading to a net decrease, or increase, in the NADH signal when workload is increased, or decreased, respectively. The somewhat slower response time of mitochondrial Ca²⁺ dynamics and activation of NADH production by the Ca²⁺ stimulation of the TCA cycle dehydrogenases contributes to the recovery of the NADH signal during the undershoot and to the NADH overshoot when workload decreases. Briefly, the NADH initial undershoot is linked to the sudden increase in respiratory rate not counterbalanced by an increased NADH production by mitochondrial dehydrogenases. Later, during the recovery phase, NADH production is activated by Ca²⁺ stimulation of the TCA cycle dehydrogenases. These remain activated even after the sudden drop in respiration that occurs when the pacing rate is decreased. This transient imbalance explains the overshoot in NADH that slowly relaxes to a lower NADH level when the mitochondrial Ca²⁺ levels decrease and dehydrogenases activation ceases.

The simultaneous regulatory effects of Ca²⁺ and ADP were further explored in the simulations shown in Fig. 7. When the rate of ATP hydrolysis by the myofibrillar ATPase was halved there was a decrease in the amplitude of the NADH transients (undershoot and overshoot) in accord with the smaller changes in ATP and ADP (Fig. 7 A: compare the *solid trace* at lower maximal ATPase rate, with the *shaded control profile*).

In contrast, if the maximal rate of the mitochondrial Ca^{2+} uniporter is decreased to 1/10th of the control value, the NADH profile resembles that obtained in the absence of stimulation of Krebs cycle dehydrogenases by Ca^{2+} (compare Figs. 7 C and 6 B). The lack of a recovery phase (evident in the *solid trace* of Fig. 7 C) is attributable to the extremely low levels of $[\operatorname{Ca}^{2+}]_m$ attained during this protocol (Fig. 7 D).

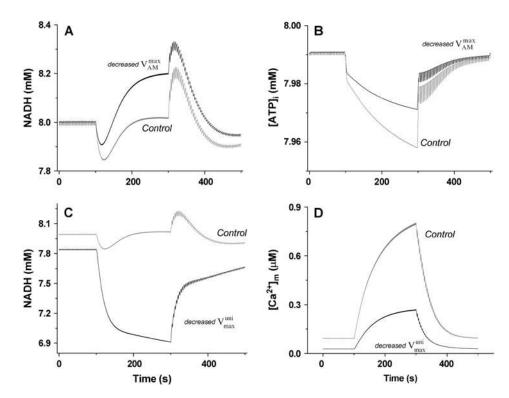


FIGURE 7 Effect of changing the myofibrillar ATPase and mitochondrial Ca2+ uniporter on the ECME model energetic behavior after changes in workload. (A) The behavior of NADH in simulations with the pacing protocol and parametric conditions as described in the legend of Fig. 5, except that the maximal rate of ATP hydrolysis by the AM-ATPase was decreased to one-half (solid $trace; V_{AM}^{max} = 3.6 \, 10^{-3} \, \, \text{mM ms}^{-1}) \, \, \text{of the}$ control value (shaded trace). (B) The profile of average ATP_i for changes in workload under control conditions (shaded trace) or with decreased myofibrillar ATPase activity (solid trace). (C) The NADH profile in model simulations with the same pacing protocol and parameters as described in the legend of Fig. 5, but with the maximal rate of the mitochondrial Ca2+ uniporter decreased to 1/10th (solid trace; $V_{\text{max}}^{\text{uni}} = 2.75 \, 10^{-3}$ mM ms⁻¹) of the control value (shaded trace). (D) The profile of $[Ca^{2+}]_m$ accumulation for the low uniporter condition described in panel C (solid trace) as compared to the control (shaded trace).

Effects of stimulation frequency on transient bioenergetic and contractile behavior

To subject the ECME model to a more comprehensive and stringent test, we monitored the dynamics of mitochondrial energetics (VO2, ADPm, NADH) and contractile work (force), as well as the two main effectors, Ca2+ and ADP_m, while the stimulatory frequency was varied over a wide range. The pacing frequency was increased from a baseline of 0.25 Hz to a higher frequency, e.g., 0.5, 1.0, 1.5, or 2.0 Hz, and returned to 0.25 Hz as indicated in the diagram at the top of Fig. 8. This in silico experiment emulates the experimental protocol reported by Brandes and Bers ((32) Fig. 8 B) and tests how changes in the average force and Ca²⁺ transport work contribute to the different phases of the mitochondrial NADH transient. ECME model simulations of the average force and the transient kinetics of the NADH profile qualitatively reproduce the experimental results (Fig. 8 A). The contractile activity drives changes in the adenine nucleotide pool and the respiratory flux (Fig. 8 C), in close correlation with the average force (Fig. $8\,A$). Fig. $8\,D$ shows how the responses of ADP_m and Ca_m^{2+} can account for the larger undershoot/overshoot and recovery phases of the NADH signal as the frequency increases.

DISCUSSION

A mathematical model was developed in which the electrical, Ca²⁺ handling and contractile properties of the cardiac myocyte were integrated with mitochondrial bioenergetics.

The ECME model is able to reproduce the pseudo-steady state and, importantly, the dynamic profile of changes in essential physiological variables such as ADP, NADH, and Ca²⁺ in cardiac myocytes subjected to changes in stimulation frequency and/or external Ca²⁺. Interactions between sarcolemmal and mitochondrial ion transport mechanisms, ATP consumption, and oxidative phosphorylation were sufficiently robust to simulate the matching of energy supply and demand over a range of workloads.

Excitation-contraction coupling/mitochondrial energetics model description

The excitation-contraction coupling/mitochondrial energetics (ECME) model is the first to integrate detailed biophysical descriptions of the activity of cardiac ion channels, sarcolemmal and mitochondrial ion transport pathways, excitation-contraction coupling, and myofilament activation with a model of mitochondrial oxidative phosphorylation. This allowed us to explore the interrelationship between the principal energy-consuming processes of the cell (i.e., contraction and ion transport) and the energy-generating system. Signaling between the cytosolic processes and mitochondrial bioenergetics was accomplished by 1), coupling the pools of high-energy phosphate intermediates in the cytoplasmic and mitochondrial compartments; and 2), linking Ca²⁺ levels in the two compartments via the mitochondrial Ca²⁺ uniporter and Na⁺/Ca²⁺ exchanger. The key to accurately simulating the dynamic and steady-state responses of

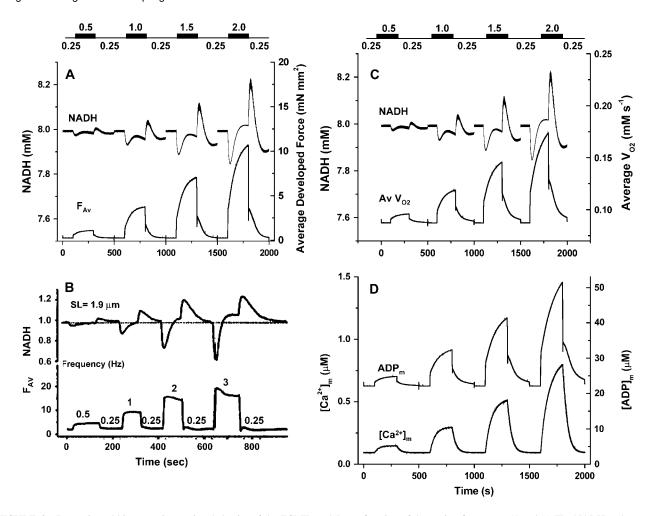


FIGURE 8 Inotropic and bioenergetic transient behavior of the ECME model as a function of the pacing frequency. (A and B) The NADH and average developed force profiles during transients in workload at various frequencies in simulations (A) and experiments (B) (from (32)). The simulation protocol consists of abrupt changes in pacing frequency from 0.25 Hz to 0.5, 1.0, 1.5, and 2.0 Hz, as indicated in the bar diagram at the top of panel A. (C) The average oxygen consumption rate (in mM s⁻¹) with the NADH profile shown for reference. (D) The time course of the two effectors of the bioenergetic machinery (average ADP_m and Ca²⁺_m) that are involved in the energetic response to a change in workload. Parameters and initial conditions are the same as those used in Figs. 3–5 Panel B was reproduced from Brandes and Bers (32) by copyright permission of the Biophysical Society.

bioenergetics to changes in workload lies in the balance between stimulation of the respiratory chain by enhanced ATP hydrolysis and stimulation of the Krebs cycle dehydrogenases. The differences in the relative response times of these two processes can account for the transient overshoot and undershoot behavior of mitochondrial NADH. Experimental evidence supporting a direct link in the response time of Krebs cycle dehydrogenases activation by mitochondrial Ca²⁺ and the recovery kinetics of NADH was provided by Brandes and Bers (17).

As in our previous model of the isolated mitochondrion (16), we have sought to reproduce the dynamic response to an abrupt change in workload as the most stringent test of the integrated model. In this regard, there have been few studies in which mitochondrial responses have been recorded in parallel with force measurements, so we have relied heavily on the data of Brandes and Bers (17), who recorded NADH

transients, mitochondrial Ca²⁺ accumulation, and force in a unbranched rat cardiac trabecula preparation. Whether this preparation accurately reproduces the time course of change of the same parameters in an in vivo setting will require comparable recordings of all the variables of interest in the intact heart.

Nevertheless, the model results demonstrate that for changes in workload induced by increasing or decreasing stimulation frequency, the NADH dynamics of the muscle can be described by the combination of ADP-dependent and Ca²⁺-dependent regulatory mechanisms. Small changes in ATP_i, and consequently in the levels of ADP in the cytoplasmic and mitochondrial compartments, mediate rapid changes in the mitochondrial NADH/NAD⁺ redox state. When ATP_i was clamped, the rapid decrease in NADH upon an increase in work was eliminated, as was the overshoot when work was decreased. In this condition, NADH

increased and decreased monotonically as workload was varied, primarily reflecting the effects of Ca²⁺ on the rate of NADH production by the Krebs cycle. In the model, the Ca²⁺-sensitive dehydrogenases IDH and KGDH exert the most control over mitochondrial NADH levels when ATP is clamped (16).

When the Ca²⁺ sensitivity of the Krebs cycle dehydrogenases was eliminated in the model, the effects of mitochondrial ADP on NADH oxidation were revealed clearly. An acute increase in average force is rapidly translated via the adenine nucleotide pool to an increase in respiration and, conversely, a decrease in work quickly results in a decrease in the rate of NADH oxidation by the respiratory chain. This raises the important question of how to model the highenergy phosphate transfer system between the sites of ATP consumption in the cytoplasm and ATP production by the mitochondria. This is a subject of ongoing debate (7) that must take into consideration the local spatial organization of the cardiomyocyte and the kinetics of the buffering reactions mediated by creatine kinase (and, ideally, other buffers like adenylate kinase as well). From first-principles, at high work load, mitochondrial ATP production has to match the approximately eightfold increase in the rate of ATP hydrolysis by the actomyosin ATPase. Hence, ADP influx across the mitochondrial inner membrane must increase in parallel. In cardiac muscle, the creatine kinase system can act as both an ATP buffer and a high-energy phosphate shuttle (39). This presents a problem in a model that does not formally incorporate spatial aspects with respect to incorporating the ability of the CK reaction to buffer the bulk cytosolic ATP concentration, while still being able to describe rapid ADP and P_i delivery to the mitochondrial adenine nucleotide and phosphate transporters, which are thought to be in a complex with the mitochondrial ATP synthase (40). As a compromise, we have included two nucleotide pools in the model, a bulk cytosolic pool that is largely buffered by the CK reaction and a pool with minimal buffering associated with the excitation-contraction coupling processes. The latter pool allows the mitochondria to rapidly and directly sense changes in energetic demand via mitochondrial ADP concentration. This representation should not be viewed as a literal description of compartmentation in the physical system, but as a construct that allowed us to simulate rapid phosphoryl (i.e., high energy phospho-group) transfer to and from the mitochondria without creating a computationally intractable spatial model of the cell (requiring partial differential equations).

Comparison of model and experimental results

The incorporation of both the ADP- and Ca²⁺-dependent regulatory mechanisms was required to adequately describe the experimental data of Brandes and Bers (32) with regard to the different effects of changes in work associated with contractile activity and the work associated with changes in

Ca2+ handling. Contractile activity can be varied in the absence of a change in average cytosolic Ca²⁺ by changing resting sarcomere length, while Ca²⁺ homeostasis can be varied by changing stimulation frequency, external Ca²⁺, or inotropic intervention (e.g., β -adrenergic receptor stimulation). In response to an increased pacing rate, mitochondrial NADH transiently decreases (phase I) and then recovers (phase II; Fig. 5 A) (32). The phase II recovery of NADH depends on the average cytosolic (and consequently mitochondrial) Ca²⁺, and the net redox state attained after equilibration to the new workload is strongly affected by the sarcomere length. As the sarcomere length approaches the optimum of the Frank-Starling curve (i.e., L_{max}), average force for any given Ca²⁺ is increased and the total energetic demand is increased, thus leading to a net oxidation of the NADH/NAD⁺ redox pool. Our simulations show that ADP_m, which reflects changes in cytosolic ADP, accounts for the initial rapid decline of NADH at the onset of high frequency stimulation (Figs. 6 B and 7 A, and Fig. 8, A and D). The rapid decrease in ADP_m as the workload is lowered also underlies the transient overshoot of NADH during the protocol. At this point, NADH production, which was accelerated by Ca²⁺ stimulation of the dehydrogenases, remains activated, while NADH oxidation decreases more rapidly. Again, the balance between the relaxation times of the demand-led and Krebs cycle processes determines the overall profile.

The effect of increasing the pacing rate in ferret hearts results in unchanged ATP levels and an initial decrease of CrP followed by a recovery to steady-state levels (if glycolysis is operating) (38). In the absence of glycolytic flux, the recovery phase of CrP is not observed and upon return to the low pacing frequency CrP level increases to reach the original steady-state levels (38). The model simulations reproduce the condition in the absence of glycolysis (Fig. 5 C) since according to the model, only mitochondrial ATP synthesis can replenish CrP. The change in Pi could not be directly computed because the operation of the adenine nucleotide translocator is carrying phosphoryl groups into the cytoplasm whose flux is counterbalanced by the phosphate carrier (not accounted for by the model). However, the main determinant of Pi dynamics in the cytosol is CrP, thus the Pi should mirror the CrP concentration profile when subjected to changes in pacing frequency (not shown).

Another agreement between our simulations and the experimental results concern the cytosolic levels of metabolites: [ATP], [NADH], [CrP], and [Ca²⁺], which are very close to the physiological values observed in ventricular myocytes of various species. As a matter of fact, NADH is highly reduced in the mitochondrial matrix (\sim 75%) (17). Since the total concentration of mitochondrial pyrimidine nucleotides is 10 mM in our model, an 80% reduction will correspond to 8 mM NADH (Fig. 5 A), which resembles the value reported (17). ATP was reported to be in the order of 7.5 mM; CrP is \sim 21 mM at low pacing frequency, and can decrease up to 15 mM (38). Ca²⁺ resting level is \sim 100–200 nM

whereas the systolic concentration can peak from 400 nM to 1 μ M (41).

A sensitivity analysis (data not shown) performed at 0.25, 1.0, and 2 Hz under the same parametric conditions as those used in the experiments shown in Figs. 3–5 revealed that the steps to which respiratory or ATP synthesis fluxes were most sensitive were localized downstream of NADH. This is in accordance with our earlier metabolic control analysis carried out for the isolated mitochondrial model (16). In the case of the integrated model, the processes that influence the rate of ATP hydrolysis are now explicitly described in a detailed physiological context, thus leading to important interdependencies between the steps that strongly influence E-C coupling and energetics.

It should be noted that Balaban and co-workers (1) have failed to observe NADH transients in intact hearts of the type reported by Brandes and Bers, leading to the notion that energy supply is rapidly increased to meet energetic demand through fast parallel activation of the respiratory chain and Krebs cycle dehydrogenases by a cytoplasmic messenger. Potential candidates for the active messenger include Ca²⁺ (12) or P_i (13), while ADP was thought to play a diminished role in the process. In isolated mitochondria, respiration was shown to respond rapidly (within hundreds of milliseconds) to changes in both Ca²⁺ and ADP (12). However, van Beek and co-workers (42) stated that the transient changes in energy fluxes and intermediates do not necessarily occur simultaneously and are altered upon inhibition of creatine kinase and/or glycolytic flux (43). The transient time was found to be much shorter for adenine nucleotides than for respiration, arguing against simultaneous parallel activation of energy production and consumption by a single, common effector (42). Further investigation into the transient dynamics of respiration, Ca²⁺, force, NADH, and ATP turnover in response to changes in cardiac workload will be required to resolve these issues. Our results indicate that Ca²⁺ and ADP, affecting mitochondrial energetics with different response times, are sufficient to reproduce available experimental data. Mixed regulation of mitochondrial energetics would potentially confer more flexibility to the heart in responding to different physiological challenges, for example, as could occur when changes in workload are elicited by variations in ADP with or without associated changes in the average cytosolic Ca²⁺ (32,44).

Directions for further model development

In taking on the challenge of incorporating most of the fundamental functional properties of the cardiac myocyte, the present integrated model is able to qualitatively reproduce the pseudo-steady state and transient responses of mitochondrial oxidative phosphorylation to changes in cardiac work. Semiquantitative agreement with the force-respiration relationship obtained in isolated cardiac trabeculae subjected

to various pacing frequencies and external Ca²⁺ concentrations was also achieved. Quantitative differences between our simulations and available experimental data can, in part, be explained by differences in the E-C coupling properties of the rat (which we choose for experiments due to the extensive validation of this preparation in our laboratory and others) and the Guinea-pig (which serves as a well established model representative of the E-C coupling properties of larger mammals) (41). The relative contributions of SERCA and the Na⁺/Ca²⁺ exchanger to the reuptake of cytoplasmic Ca²⁺ after the peak are different in rats and guinea-pigs. As a consequence, the fraction of Ca²⁺ that is recycled is much larger in rats than in guinea-pigs. The rat trabeculae experiments were carried out at 22°C whereas the model parameters were adjusted for currents and fluxes operating at 37°C. This is another source of variation and further experimentation with different species and temperature will be required to determine their contribution to quantitative discrepancies with the model.

The feasibility of ADP and Ca²⁺ as important mediators of energy supply and demand matching has been demonstrated in the present model, but this work does not preclude the possibility that other mechanisms/mediators might be involved. For example, compelling evidence exists that various steps in the electron transport chain may be regulated by allosteric mechanisms (45), which would be replicated in our model by changing the concentration of respiratory carriers (ρ^{res}) in response to changes in work. Since the rate of the mitochondrial ATP synthase is governed by the protonmotive force and the availability of ADP and P_i, independently of the rate of respiration, we have observed in some simulations that ATP synthesis outpaces the increase in respiration, resulting an increase in the P/O ratio at high work (P/O ratio refers to the quotient of the ATP synthesis rate over the respiratory rate and represents a measure of the efficiency of oxidative phosphorylation). This changing P/O ratio differs from experimental results obtained in isolated rat hearts (46), perhaps suggesting an avenue for further refinement and validation of the model.

Cytosolic Ca²⁺ handling in the E-C coupling module has been previously validated by simulating the short-term interval force relations of cardiac muscle (15,47). The experimentally observed behavior of restitution and post-extrasystolic potentiation (48) are also appropriately reproduced in the integrated model (see Supplementary Material, Fig. S4). According to the model, Na⁺ levels determine, to a certain extent, the level of Ca²⁺ and the rate of Ca²⁺ removal through the Na⁺,Ca²⁺ exchanger activity. This is reflected by the accumulation of Na⁺ as frequency increases (see Supplementary Material, Fig. S2). Nevertheless, we have not accounted yet for important processes influencing cytosolic Na⁺ levels such as the Na⁺,H⁺ exchanger, which may render a more accurate picture of this cation.

A more controversial issue is to what extent the mitochondria will influence the cytosolic Ca²⁺ transient and how

rapidly Ca^{2+} is taken up by the mitochondria (49). Indeed, we (50) and others (49,51) have obtained evidence that Ca^{2+} may be taken up rapidly by the mitochondria during the Ca^{2+} transient. This again raises the question of the spatial organization of the components of the model, as mentioned above when considering high-energy phosphate transfer rates. This is another area that will likely require further refinement of the model and experimentation. As formulated in this study, the mitochondria responded to the bulk cytoplasmic Ca^{2+} concentration and did not substantially alter the Ca^{2+} -induced Ca^{2+} release process of the junctional space.

Comparison with other mathematical models

There have been few previous attempts to develop computational models linking electrophysiology, ion homeostasis, Ca²⁺ handling, ATP consumption, and mitochondrial energetics. Magnus and Keizer (52) developed a model that incorporated plasmalemmal ion channels, Ca^{2+} handling, and ATP production by glycolysis and mitochondria to simulate the bursting behavior of pancreatic β -cells. Elements of that model were used as components of our previous isolated cardiac mitochondrial model (16), with extensive modifications including the addition of NADH as a state variable, dependent on the activity of the Krebs cycle. In the present model, both Ca²⁺ and ADP are now variables that depend on the sum total of physiological processes associated with E-C coupling and mitochondrial function. The only remaining important fixed influx is the supply of Acetyl CoA to the Krebs cycle, which could be refined in the future by incorporating established models of glycolysis and β -oxidation of fatty acids. This could account for potential limitations of higher-order substrate supply, which could be relevant to the simulation of pathological conditions.

Another recent model based on a sound electrophysiological formulation focused on the interactions between the mitochondrial and cytoplasm space with Ca²⁺ as the sole signaling molecule (53). Presumably owing to the lack of significant respiratory control in the mitochondrial component of this model (54), the interrelationship between a change in E-C coupling and bioenergetics is not well described.

Saks and collaborators (7,9,55,56) have also modeled the energetic processes linked to muscle contraction, but they did not take into account the electrophysiology of the cell. Their model was more oriented to processes occurring in the cytoplasm and mitochondrial intermembrane space, including creatine kinase and adenylate kinase and was intended to address the some of the spatial aspects of phosphoryl transfer that we have discussed above. Force generation in this model was an adjustable function used to calculate its contribution to energy consumption rather than as a biophysical description of contraction.

Concluding remarks

We have developed an integrated model of the electrophysiology, E-C coupling properties, and mitochondrial bioenergetic responses of the cardiac myocyte. The model reproduces the pseudo steady-state force-respiration relationship and is also capable of describing the transient energetic responses to abrupt changes in workload. The ECME model can be used to explore the important interactions between the electrical, contractile metabolic functions of the heart, which will lead to an improved quantitative understanding of cardiac physiology under normal or pathological conditions.

APPENDIX

Ionic currents

Fast Na⁺ current (I_{Na})

$$I_{\text{Na}} = \bar{G}_{\text{Na}} m^3 h j \left(V - E_{\text{Na}} \right), \tag{A1}$$

$$E_{\text{Na}} = \frac{RT}{F} \ln \left(\frac{[\text{Na}^+]_{\text{o}}}{[\text{Na}^+]_{\text{i}}} \right), \tag{A2}$$

$$\frac{dm_{\text{Na}}}{dt} = \alpha_{\text{m}}(1 - m_{\text{Na}}) - \beta_{\text{m}}m_{\text{Na}}, \tag{A3}$$

$$\frac{dh_{\text{Na}}}{dt} = \alpha_{\text{h}}(1 - h_{\text{Na}}) - \beta_{\text{h}}h_{\text{Na}},\tag{A4}$$

$$\frac{dj_{\text{Na}}}{dt} = \alpha_{\text{j}}(1 - j_{\text{Na}}) - \beta_{\text{j}}j_{\text{Na}},\tag{A5}$$

$$\alpha_{\rm m} = 0.32 \frac{V + 47.13}{1 - e^{-0.1(V + 47.13)}},$$
 (A6)

$$\beta_{\rm m} = 0.08 \, e^{-V/11}.\tag{A7}$$

For $V \ge -40 \text{ mV}$

$$\alpha_{\rm h} = 0.0,\tag{A8}$$

$$\alpha_{\rm i} = 0.0,\tag{A9}$$

$$\beta_{\rm h} = \left(0.13\left(1 + e^{\left(\frac{V + 10.66}{-11.1}\right)}\right)\right)^{-1},$$
 (A10)

$$\beta_{\rm j} = 0.3 \frac{e^{-2.535 \times 10^{-7} \rm V}}{1 + e^{-0.1(\rm V + 32)}}.$$
 (A11)

For V < -40 mV

$$\alpha_{\rm h} = 0.135 \, e^{\frac{80 + \rm V}{-6.8}},$$
 (A12)

$$\alpha_{\rm j} = (-127, 140 \, e^{0.2444 \,\rm V} - 3.474 \times 10^{-5} \, e^{-0.04391 \,\rm V}) \times \frac{V + 37.78}{1 + e^{0.311 \,\rm (V + 79.23)}}, \tag{A13}$$

$$\beta_{\rm h} = 3.56 e^{0.079V} + 3.1 \times 10^5 e^{0.35V},$$
 (A14)

$$\beta_{\rm j} = 0.1212 \frac{e^{-0.01052V}}{1 + e^{-0.1378(V + 40.14)}}.$$
 (A15)

See Table 1.

Time-dependent delayed rectifier K⁺ current (I_K)

$$I_{\rm K} = \bar{G}_{\rm K} X_1 X^2 (V - E_{\rm K}),$$
 (A16)

$$E_{K} = \frac{RT}{F} \ln \left(\frac{[K^{+}]_{o} + P_{Na,K}[Na^{+}]_{o}}{[K^{+}]_{i} + P_{Na,K}[Na^{+}]_{i}} \right), \quad (A17)$$

$$\bar{G}_{\rm K} = 0.282 \sqrt{\frac{{\rm [K^+]}_{\rm o}}{5.4}},$$
 (A18)

$$X_1 = (1 + e^{(V-40)/40})^{-1},$$
 (A19)

$$\frac{dX}{dt} = \alpha_{\chi}(1 - X) - \beta_{\chi}X,\tag{A20}$$

$$\alpha_{\chi} = 7.19 \, 10^{-5} \frac{V + 30}{1 - e^{-0.148(V + 30)}},$$
 (A21)

$$\beta_{\chi} = 1.31 \, 10^{-4} \frac{V + 30}{-1 + e^{0.0687(V + 30)}}.$$
 (A22)

Time-independent K⁺ current (I_{K1})

$$I_{K_1} = \bar{G}_{K_1} K_{1 \infty} (V - E_{K_1}), \tag{A23}$$

$$E_{K_1} = \frac{RT}{F} \ln \left(\frac{[K^+]_o}{[K^+]_i} \right), \tag{A24}$$

TABLE 1 General parameters

Symbol	Value	Units	Description	Eq.	Refs.
F	96.5	C mmol ⁻¹	Faraday constant.		
T	310	K	Absolute temperature.		
R	8.314	$\mathrm{J} \; \mathrm{mol}^{-1} \; \mathrm{K}^{-1}$	Universal gas constant.		
C_{m}	1.0	$\mu \mathrm{F \ cm}^{-2}$	Membrane capacitance.	A79	(14)
$A_{\rm cap}$	$1.534 \ 10^{-4}$	cm ²	Capacitative cell surface area.	A88	(14)
$V_{ m myo}$	25.84	pL	Cytosolic volume.	A88	(14)
$V_{ m mito}$	15.89	pL	Mitochondrial volume.	A92	(57)
$V_{ m NSR}$	1.4	pL	NSR volume.	A91	(15)
$V_{ m JSR}$	0.16	pL	JSR volume.	A89	(15)
V_{SS}	$0.495 \ 10^{-3}$	pL	SS volume.	A89	(15)
$[K^+]_o$	5.4	mM	Extracellular K ⁺ concentration.	A17	(14)
[Na ⁺] _o	140.0	mM	Extracellular Na ⁺ concentration.	A2	(14)
[Ca ²⁺] _o	2.0	mM	Extracellular Ca ²⁺ concentration.	A32	(14)

$$\bar{G}_{K_1} = 0.75 \sqrt{\frac{[K^+]_o}{5.4}},$$
 (A25)

$$K_{1\infty} = \frac{\alpha_{K_1}}{\alpha_{K_1} + \beta_{K_1}},$$
 (A26)

$$\alpha_{K_1} = \frac{1.02}{1 + e^{0.2385(V - E_{K_1} - 59.215)}},$$
(A27)

$$\beta_{K_1} = \frac{0.4912 \, e^{0.08032(V - E_{K_1} + 5.476)} + e^{0.06175(V - E_{K_1} - 594.31)}}{1 + e^{-0.5143(V - E_{K_1} + 4.753)}}. \quad (A28)$$

Plateau K⁺ current (I_{Kp})

$$I_{K_{\rm D}} = \bar{G}_{K_{\rm D}} K_{\rm P} (V - E_{K_{\rm D}}),$$
 (A29)

$$E_{K_{P}} = E_{K_{1}}, \tag{A30}$$

$$K_{\rm p} = (1 + e^{(7.488 - {\rm V})/5.98})^{-1}.$$
 (A31)

Na⁺/Ca²⁺ exchanger current (I_{NaCa})

$$I_{\text{NaCa}} = k_{\text{NaCa}} \frac{1}{K_{\text{m,Na}}^{3} + [\text{Na}^{+}]_{\text{o}}^{3}} \frac{1}{K_{\text{m,Ca}} + [\text{Ca}^{2+}]_{\text{o}}} \times \left(1 + k_{\text{sat}} e^{(\eta - 1)\frac{\text{VF}}{\text{RT}}}\right)^{-1}$$

$$\times \left\{ e^{\eta_{RT}^{YF}} [Na^{+}]_{i}^{3} [Ca^{2+}]_{o} - e^{(\eta-1)\frac{VF}{RT}} [Na^{+}]_{o}^{3} [Ca^{2+}]_{i} \right\}. \tag{A32}$$

See Table 2.

Na⁺, K⁺ pump current (I_{NaK})

$$I_{\text{NaK}} = \bar{I}_{\text{NaK}} f_{\text{NaK}} f_{\text{NaK}}^{\text{ATP}} \left(1 + \left(\frac{K_{\text{m,Na}_{i}}}{\left[\text{Na}^{+} \right]_{i}} \right)^{1.5} \right)^{-1} \frac{\left[\text{K}^{+} \right]_{\text{o}}}{\left[\text{K}^{+} \right]_{\text{o}} + K_{\text{m,K}_{o}}}, \tag{A33}$$

$$f_{\text{NaK}} = \left(1 + 0.1245 e^{-0.1\frac{\text{VE}}{\text{RT}}} + 0.0365 e^{-\frac{\text{VE}}{\text{RT}}} \left(\frac{e^{[\text{Na}^+]_{\text{o}}/67.3} - 1}{7}\right)\right)^{-1},$$
(A34)

$$f_{\text{NaK}}^{\text{ATP}} = \left(1 + \frac{K_{\text{NaK}}^{1, \text{ATP}}}{[\text{ATP}]_{i}} \left(1 + \frac{[\text{ADP}]_{i}}{K_{\text{NaV}}^{i, \text{ADP}}}\right)^{-1}.$$
 (A35)

See Table 3.

TABLE 2 Membrane current parameters

Symbol	Value	Units	Description	Eq.	Refs.
$\overline{\overline{G}}_{Na}$	12.8	mS μ F ⁻¹	Maximal Na channel conductance.	A1	(14)
\overline{G}_{K_P}	8.28×10^{-3}	mS μF^{-1}	Maximal plateau K channel conductance.	A29	(14)
$P_{\mathrm{Na,K}}$	0.01833		Na ⁺ permeability of K ⁺ channel.	A17	(14)
$k_{ m NaCa}$	9000	$\mu A \mu F^{-1}$	Scaling factor of Na ⁺ /Ca ⁺ exchange.	A32	(15)
$k_{\rm m,Na}$	87.5	mM	Na half-saturation constant NCX.	A32	(14)
$k_{\rm m,Ca}$	1.38	mM	Na half-saturation constant NCX.	A32	(14)
$k_{\rm sat}$	0.1		Na ⁺ /Ca ²⁺ exchange saturation factor at negative potentials.	A32	(14)
η	0.35		Controls voltage dependence of NCX.	A32	(14)

Nonspecific Ca²⁺ activated current (I_{ns(Ca)})

$$I_{\rm ns(Ca)} = I_{\rm ns(Na)} + I_{\rm ns(K)},$$
 (A36)

$$I_{\text{ns(Na)}} = \bar{I}_{\text{ns(Na)}} \left(1 + \left[\frac{K_{\text{m,ns(Ca)}}}{\left[\text{Ca}^{2+} \right]_{\text{i}}} \right]^{3} \right)^{-1},$$
 (A37)

$$\bar{I}_{\rm ns(Na)} = P_{\rm ns(Na)} \frac{VF^2}{RT} \frac{0.75([{\rm Na}^+]_{\rm i} e^{{\rm VF/RT}} - [{\rm Na}^+]_{\rm o})}{e^{{\rm VF/RT}} - 1}, \quad (A38)$$

$$I_{\text{ns(K)}} = \bar{I}_{\text{ns(K)}} \left(1 + \left[\frac{K_{\text{m,ns(Ca)}}}{\left[\text{Ca}^{2+} \right]_{i}} \right]^{3} \right)^{-1},$$
 (A39)

$$\bar{I}_{\text{ns(K)}} = P_{\text{ns(K)}} \frac{VF^2}{RT} \frac{0.75([K^+]_i e^{VF/RT} - [K^+]_o)}{e^{VF/RT} - 1}.$$
 (A40)

Background Ca²⁺ current (I_{Ca,b})

$$I_{\text{Ca,b}} = \bar{G}_{\text{Ca,b}}(V - E_{\text{Ca,N}}),$$
 (A41)

TABLE 3 Na⁺/K⁺ pump parameters

Symbol	Value	Units	Description	Eq.	Refs.
$ar{I}_{ m NaK}$	3.147	μ A μ F ⁻¹	Maximum Na ⁺ /K ⁺ pump current.	A33	*
$K_{\rm m,Nai}$	10	mM	Na half-saturation for Na ⁺ /K ⁺ pump.	A33	(14)
$K_{\rm m,Ko}$	1.5	mM	K half-saturation for Na ⁺ /K ⁺ pump.	A33	(14)
$K_{ m NaK}^{1, m ATP}$	8.0×10^{-3}	mM	ATP half-saturation constant for	A35	(21)
$K_{ m NaK}^{ m i,ADP}$	0.1	mM	Na ⁺ /K ⁺ pump. ADP inhibition constant for Na ⁺ /K ⁺ pump.	A35	(21)

^{*}Adjusted based on the value of Na⁺ concentration to match physiological levels (58,59).

$$E_{\text{Ca,N}} = \frac{RT}{2F} \ln \left(\frac{[\text{Ca}^{2+}]_{\text{o}}}{[\text{Ca}^{2+}]_{\text{i}}} \right).$$
 (A42)

Background Na⁺ current (I_{Na,b})

$$I_{\text{Na.b}} = \bar{G}_{\text{Na,b}}(V - E_{\text{Na,N}}),$$
 (A43)

$$E_{\text{Na,N}} = E_{\text{Na}}.\tag{A44}$$

See Tables 4 and 5.

Sarcolemmal Ca²⁺ pump current (I_{pCa})

$$I_{\text{pCa}} = I_{\text{pCa_max}} F_{\text{pCa}}^{\text{ATP}} \frac{[\text{Ca}^{+2}]_{\text{i}}}{K_{\text{m}}^{\text{pCa}} + [\text{Ca}^{+2}]_{\text{i}}}, \tag{A45}$$

$$F_{pCa}^{ATP} = \left(1 + \frac{K_{m1_pCa}^{ATP}}{[ATP]_{i}} \left(1 + \frac{[ADP]_{i}}{K_{i_pCa}^{ADP}}\right)\right)^{-1} + \left(1 + \frac{K_{m2_pCa}^{ATP}}{[ATP]_{i}}\right)^{-1}.$$
(A46)

See Table 6.

SERCA pump (J_{up})

$$J_{\rm up} = \frac{V_{\rm maxr} f_{\rm b} - V_{\rm maxr} r_{\rm b}}{1 + f_{\rm b} + r_{\rm b}} f_{\rm ATP}^{\rm SERCA}, \tag{A47}$$

$$f_{\rm b} = \left(\frac{\left[{\rm Ca}^{2^+}\right]_{\rm i}}{K_{\rm fb}}\right)^{\rm Nfb},$$
 (A48)

$$r_{\rm b} = \left(\frac{\left[\text{Ca}^{2^+}\right]_{\text{NSR}}}{K_{\rm rb}}\right)^{\text{Nrb}},\tag{A49}$$

$$f_{\text{ATP}}^{\text{SERCA}} = \left(\frac{K_{\text{m,up}}^{\text{ATP}}}{\left[\text{ATP}\right]_{\text{i}}} \left(1 + \frac{\left[\text{ADP}\right]_{\text{i}}}{K_{\text{i,up}}}\right) + \left[1 + \frac{\left[\text{ADP}\right]_{\text{i}}}{K'_{\text{i,up}}}\right]\right)^{-1}.$$
(A50)

See Table 7.

TABLE 4 Nonspecific channel current parameters

Symbol	Value	Units	Description	Eq.	Refs.
$P_{\rm ns(Na)}$	1.75×10^{-7}	cm s ⁻¹	Nonspecific channel	A38	(26)
$K_{m,ns(Ca)}$	1.2×10^{-3}	mM	current Na permeability. Ca ²⁺ half-saturation c onstant for nonspecific	A37	(14)
$P_{\rm ns(K)}$	0	${\rm cm~s}^{-1}$	current. Nonspecific channel current K permeability.	A40	(15)

TABLE 5 Background Ca²⁺ current parameters

Symbol	Value	Units	Description	Eq.	Refs.
$ar{ar{G}}_{ ext{Ca,b}}$	3.217×10^{-3}	mS μ F ⁻¹	Maximum background current Ca ²⁺ conductance.	A41	*
$ar{G}_{ ext{Na,b}}$	5.45×10^{-4}	mS μ F ⁻¹	Maximum background current Na ⁺ conductance.	A43	*

^{*}Adjusted from Jafri et al. (14) and Rice et al. (15), based on physiological levels of Ca²⁺ and Na⁺ in cardiomyocytes (41,58).

L-type Ca²⁺ current (I_{Ca})

$$\alpha = 0.4 \, e^{(V+2)/10},\tag{A51}$$

$$\beta = 0.05 \, e^{-(V+2)/13},\tag{A52}$$

$$\alpha' = a \alpha, \tag{A53}$$

$$\beta' = \frac{\beta}{b},\tag{A54}$$

$$\gamma = 0.1875 \left[\text{Ca}^{2+} \right]_{\text{ss}},$$
 (A55)

$$\frac{dC_{\rm o}}{dt} = \beta C_1 + \omega C_{\rm CaO} - (4\alpha + \gamma)C_{\rm o}, \tag{A56}$$

$$\frac{dC_1}{dt} = 4\alpha C_0 + 2\beta C_2 + \frac{\omega}{b} C_{\text{Cal}} - (\beta + 3\alpha + a\gamma)C_1, \text{ (A57)}$$

$$\frac{dC_2}{dt} = 3\alpha C_1 + 3\beta C_3 + \frac{\omega}{b^2} C_{\text{Ca2}} - (2\beta + 2\alpha + a^2 \gamma) C_2,$$
(A58)

$$\frac{dC_3}{dt} = 2\alpha C_2 + 4\beta C_4 + \frac{\omega}{b^3} C_{\text{Ca3}} - (3\beta + \alpha + a^3 \gamma) C_3,$$
(A59)

$$\frac{dC_4}{dt} = \alpha C_3 + g O + \frac{\omega}{b^4} C_{\text{Ca4}} - (4\beta + f + a^4 \gamma) C_4, \quad (A60)$$

TABLE 6 Sarcolemmal Ca2+ current parameters

Symbol	Value	Units	Description	Eq.	Refs.
I_{pCa_max}	0.575	$\mu A \mu F^{-1}$	Maximum sarcolemmal Ca ²⁺ pump current.	A45	(15)
$K_{ m m}^{ m pCa}$	5×10^{-4}	mM	Ca ²⁺ half-saturation constant for sarcolemmal Ca ²⁺ pump.	A45	(14)
$K_{\rm m1_pCa}^{\rm ATP}$	0.012	mM	First ATP half-saturation constant for sarcolemmal Ca ²⁺ pump.	A46	(60)
$K_{\text{m2_pCa}}^{\text{ATP}}$	0.23	mM	Second ATP half-saturation constant for sarcolemmal Ca ²⁺ pump.	A46	(60)
$K_{i_pCa}^{ADP}$	1.0	mM	ADP inhibition constant for sarcolemmal Ca ²⁺ pump.	A46	(29)

TABLE 7 Sarcoplasmic reticulum Ca2+ ATPase parameters

Symbol	Value	Units	Description	Eq.	Refs
$V_{ m max,f}$	2.989×10^{-4}	ms^{-1}	SERCA forward rate parameter.	A47	(14)
$V_{\rm max,r}$	3.179×10^{-4}	ms^{-1}	SERCA reverse rate parameter.	A47	(14)
K_{fb}	2.4×10^{-4}	mM	Forward Ca ²⁺ half-saturation constant of SERCA.	A48	(15)
$K_{ m rb}$	1.64269	mM	Reverse Ca ²⁺ half-saturation constant of SERCA.	A49	(15)
N_{fb}	1.4		Forward cooperativity constant of SERCA.	A48	(15)
$N_{ m rb}$	1.0		Reverse cooperativity constant of SERCA.	A49	(15)
$K_{\mathrm{m,up}}^{\mathrm{ATP}}$	0.01	mM	ATP half-saturation constant for SERCA.	A50	(21)
$K_{i,up}$	0.14	mM	ADP first inhibition constant for SERCA.	A50	(21)
$K'_{i,up}$	5.1	mM	ADP second inhibition constant for SERCA.	A50	(21)

$$\frac{dO}{dt} = f C_4 - g O, \tag{A61}$$

$$\frac{dC_{\text{Ca0}}}{dt} = \beta' C_{\text{Ca1}} + \gamma C_0 - (4\alpha' + \omega) C_{\text{Ca0}}, \quad (A62)$$

$$\frac{dC_{\text{Cal}}}{dt} = 4\alpha' C_{\text{CaO}} + 2\beta' C_{\text{Ca2}} + a\gamma C_1 - \left(\beta' + 3a' + \frac{\omega}{b}\right) C_{\text{Cal}},$$
(A63)

$$\frac{dC_{\text{Ca2}}}{dt} = 3\alpha' C_{\text{Ca1}} + 3\beta' C_{\text{Ca3}} + a^2 \gamma C_2 - \left(2\beta' + 2\alpha' + \frac{\omega}{b^2}\right) C_{\text{Ca2}},$$
(A64)

$$\frac{dC_{\text{Ca3}}}{dt} = 2\alpha' C_{\text{Ca2}} + 4\beta' C_{\text{Ca4}} + a^3 \gamma C_3 - \left(3\beta' + \alpha' + \frac{\omega}{b^3}\right) C_{\text{Ca3}},$$
(A65)

$$\frac{dC_{\text{Ca4}}}{dt} = \alpha' C_{\text{Ca3}} + g' O_{\text{Ca}} + a^4 \gamma C_4 - \left(4\beta' + f' + \frac{\omega}{b^4}\right) C_{\text{Ca4}},$$
(A66)

$$\frac{dO_{\text{Ca}}}{dt} = f'C_{\text{Ca4}} - g'O_{\text{Ca}},\tag{A67}$$

$$I_{\text{Ca}_{\text{max}}} = 4\overline{P}_{\text{Ca}} \frac{VF^2}{RT} \frac{0.001 e^{2VF/\text{RT}} - 0.341 \left[\text{Ca}^{2^+}\right]_{\text{o}}}{e^{2V/\text{RT}} - 1}, \quad (A68)$$

$$I_{\text{Ca}} = 6I_{\text{Camax}} \text{ y[O]}, \tag{A69}$$

$$I_{\text{Ca,K}} = P'_{\text{K}} y [\text{O} + \text{O}_{\text{Ca}}] \frac{VF^2}{RT} \frac{[\text{K}^+]_i e^{\text{VF/RT}} - [\text{K}^+]_o}{e^{\text{VF/RT}} - 1},$$
 (A70)

$$P_{K}' = \frac{\overline{P}_{K}}{1 + \frac{I_{\text{Ca}_{\text{max}}}}{I_{Ca_{\text{bod}}}}},$$
(A71)

$$\frac{dy}{dt} = \frac{y_{\infty} - y}{\tau_{y}},\tag{A72}$$

$$y_{\infty} = \frac{1}{1 + e^{(V+55)/7.5}} + \frac{0.5}{1 + e^{(-V+21)/6}},$$
 (A73)

$$\tau_{y} = 20 + \frac{600}{1 + e^{(V+30)/9.5}}.$$
 (A74)

See Table 8.

Ca^{2+} release channel current (J_{rel})

$$\frac{dP_{\rm CI}}{dt} = -k_{\rm a}^{+} \left[{\rm Ca}^{2+} \right]_{\rm ss}^{\rm n} P_{\rm CI} + k_{\rm a}^{-} P_{\rm OI}, \tag{A75}$$

$$\frac{dP_{\text{O1}}}{dt} = k_a^+ \left[\text{Ca}^{2+} \right]_{\text{ss}}^{\text{n}} P_{\text{C1}} - k_a^- P_{\text{O1}} - k_b^+ \left[\text{Ca}^{2+} \right]_{\text{ss}}^{\text{m}} P_{\text{O1}}
+ k_b^- P_{\text{O2}} - k_b^+ P_{\text{O1}} + k_a^- P_{\text{C2}},$$
(A76)

$$\frac{dP_{O2}}{dt} = k_b^+ \left[\text{Ca}^{2+} \right]_{ss}^{m} P_{O1} - k_b^- P_{O2}, \tag{A77}$$

$$\frac{dP_{\rm C2}}{dt} = k_{\rm c}^{+} P_{\rm O1} - k_{\rm c}^{-} P_{\rm C2},\tag{A78}$$

$$J_{\text{rel}} = v_1 (P_{O_1} + P_{O_2}) ([Ca^{2+}]_{ISR} - [Ca^{2+}]_{SS}).$$
 (A79)

See Table 9.

Sarcolemmal membrane potential

$$\frac{dV}{dt} = -\frac{1}{C_{\rm m}} (I_{\rm Na} + I_{\rm Ca} + I_{\rm Ca,K} + I_{\rm K} + I_{\rm K_1} + I_{\rm Kp} + I_{\rm NaCa}
+ I_{\rm NaK} + I_{\rm ins(Ca)} + I_{\rm pCa} + I_{\rm Ca,b} + I_{\rm Na,b}).$$
(A80)

TABLE 8 L-type Ca²⁺ current parameters

Symbol	Value	Units	Description	Eq.	Refs.
A	2.0		Mode transition	A53	(14)
В	2.0		parameter. Mode transition parameter.	A54	(14)
ω	0.01	ms^{-1}	Mode transition parameter.	A56	(14)
f	0.3	ms^{-1}	Transition rate into open state.	A61	(14)
g	2.0	ms^{-1}	Transition rate out of open state.	A61	(14)
f	0.0	ms^{-1}	Transition rate into open state, mode Ca.	A67	(14)
g'	0.0	ms^{-1}	Transition rate out open state, mode Ca.	A67	(14)
$ar{P}_{\mathrm{Ca}}$	1.24×10^{-3}	${\rm cm}\ {\rm s}^{-1}$	L-type Ca ²⁺ channel permeability to Ca ²⁺ .	A68	(15)
\bar{P}_{K}	1.11×10^{-11}	${\rm cm}\ {\rm s}^{-1}$	L-type Ca ²⁺ channel permeability to K ⁺ .	A71	(15)
$I_{\mathrm{Ca_{half}}}$	-0.4583	$\mu A \mu F^{-1}$	ICa level that reduces \bar{P}_{K} by half.	A71	(15)

TABLE 9 Ca²⁺ release channel current parameters

Symbol	Value	Units	Description	Eq.	Refs.
v_1	3.6	ms ⁻¹	RyR flux channel constant.	A79	(15)
n	4		Cooperativity parameter.	A75	(14)
m	3		Cooperativity parameter.	A76	(14)
k_{a}^{+}	1.215×10^{10}	$\mathrm{mM}^{-4}~\mathrm{ms}^{-1}$	RyR rate constant.	A75	(14)
k_a^-	0.576	ms^{-1}	RyR rate constant.	A75	(61)
$k_{\rm b}^+$	4.05×10^{6}	$\mathrm{mM}^{-3}~\mathrm{ms}^{-1}$	RyR rate constant.	A76	(14)
$k_{\rm b}^-$	1.93	ms^{-1}	RyR rate constant.	A76	(14)
k_c^+	0.1	ms^{-1}	RyR rate constant.	A76	(61)
k_{a}^{+} k_{a}^{-} k_{b}^{+} k_{b}^{-} k_{c}^{+} k_{c}^{-}	8.0×10^{-4}	ms^{-1}	RyR rate constant.	A76	(14)

Ca²⁺ buffering and diffusive transport between compartments

$$J_{\text{trpn}} = \frac{d[\text{HTRPNCa}]}{dt} + \frac{d[\text{LTRPNCa}]}{dt},$$
 (A81)

$$J_{\rm tr} = \frac{[{\rm Ca}^{2+}]_{\rm NSR} - [{\rm Ca}^{2+}]_{\rm JSR}}{\tau_{\rm tr}},$$
 (A82)

$$J_{xfer} = \frac{[Ca^{2+}]_{SS} - [Ca^{2+}]_{i}}{\tau_{xfer}},$$
 (A83)

$$\beta_{i} = \left(1 + \frac{K_{m}^{CMDN}[CMDN]_{tot}}{(K_{m}^{CMDN} + [Ca^{2+}]_{i})^{2}}\right)^{-1},$$
(A84)

$$\beta_{SS} = \left(1 + \frac{K_{\rm m}^{\rm CMDN}[{\rm CMDN}]_{\rm tot}}{(K_{\rm m}^{\rm CMDN} + [{\rm Ca}^{2^+}]_{SS})^2}\right)^{-1},$$
 (A85)

$$\beta_{\rm JSR} = \left(1 + \frac{K_{\rm m}^{\rm CSQN} [{\rm CSQN}]_{\rm tot}}{(K_{\rm m}^{\rm CSQN} + [{\rm Ca}^{2+}]_{\rm ISP})^2}\right)^{-1},\tag{A86}$$

$$\frac{d[\text{HTRPNCa}]}{dt} = k_{\text{htrpn}}^{+} \left[\text{Ca}^{2^{+}} \right]_{i} ([\text{HTRPN}]_{\text{tot}} - [\text{HTRPNCa}]) - k_{\text{htrpn}}^{-} \left[\text{HTRPNCa} \right], \tag{A87}$$

$$\frac{d[\text{LTRPNCa}]}{dt} = k_{\text{ltrpn}}^{+} \left[\text{Ca}^{2+}\right]_{i} \left(\left[\text{LTRPN}\right]_{\text{tot}} - \left[\text{LTRPNCa}\right]\right) - k_{\text{ltrpn}}^{-} \left(1 - \frac{2}{3}Force_{\text{Norm}}\right) \left[\text{LTRPNCa}\right]. \tag{A88}$$

See Table 10.

Ionic concentrations in various compartments

$$\begin{split} \frac{d[\mathrm{Ca}^{2^{+}}]_{\mathrm{i}}}{dt} &= \beta_{\mathrm{i}} \bigg[J_{\mathrm{xfer}} - J_{\mathrm{up}} - J_{\mathrm{trpn}} - (I_{\mathrm{Ca,b}} - 2I_{\mathrm{NaCa}} + I_{\mathrm{pCa}}) \frac{A_{\mathrm{cap}}}{2V_{\mathrm{myo}}F} \\ &+ (V_{\mathrm{NaCa}} - V_{\mathrm{uni}}) \frac{V_{\mathrm{mito}}}{V_{\mathrm{myo}}} \bigg], \end{split} \tag{A89}$$

TABLE 10 Ca²⁺ transport and buffering parameters

Symbol	Value	Units	Description	Eq. Refs.
$ au_{ m tr}$	0.5747	ms	Time constant for transfer from subspace to myoplasm.	A82 (15)
$ au_{ ext{xfer}}$	9.09	ms	Time constant for transfer from NSR to JSR.	A83 (15)
$K_{\rm m}^{ m CMDN}$	2.38×10^{-3}	mM	Ca ²⁺ half saturation constant for	A84 (15)
$K_{\rm m}^{\rm CSQN}$	0.8	mM	calmodulin. Ca ²⁺ half saturation constant for	A85 (15)
$k_{ m htrpn}^+$	100	$\mathrm{mM}^{-1}~\mathrm{ms}^{-1}$	calsequestrin. Ca ²⁺ on-rate for troponin	A86 (15)
k_{htrpn}^{-}	$3.3 \ 10^{-4}$	ms^{-1}	high-affinity sites. Ca ²⁺ off-rate for troponin	A87 (15)
k_{ltrpn}^+	100	$\mathrm{mM}^{-1}~\mathrm{ms}^{-1}$	high-affinity sites. Ca ²⁺ on-rate for troponin	A88 *
k_{ltrpn}^{-}	4×10^{-2}	ms^{-1}	low-affinity sites. Ca ²⁺ off-rate for troponin low-affinity sites.	A88 (14)
[HTRPN] _{tot}	0.14	mM	Total troponin high-affinity sites.	A87 (14)
[LTRPN] _{tot}	0.07	mM	Total troponin low-affinity sites.	A88 (14)
[CMDN] _{tot}	5.0×10^{-2}	mM	Total myoplasmic calmodulin concentration.	A84 (14)
[CSQN] _{tot}	15	mM	Total NSR calsequestrin concentration.	A85 (15)

^{*}Adjusted from the value reported in Rice et al. (15) to reproduce the values of the developed force by ventricular guinea-pig muscles, as described in Ruf et al. (62).

$$\frac{d[\text{Ca}^{2^{+}}]_{\text{ss}}}{dt} = \beta_{\text{ss}} \left[J_{\text{rel}} \frac{V_{\text{JSR}}}{V_{\text{ss}}} - J_{\text{xfer}} \frac{V_{\text{myo}}}{V_{\text{ss}}} - (I_{\text{Ca}}) \frac{A_{\text{cap}}}{2V_{\text{ss}}F} \right], \quad (A90)$$

$$\frac{d[\text{Ca}^{2^{+}}]_{\text{JSR}}}{dt} = \beta_{\text{JSR}} [J_{\text{tr}} - J_{\text{rel}}], \quad (A91)$$

$$\frac{d[\operatorname{Ca}^{2+}]_{NSR}}{dt} = J_{up} \frac{V_{myo}}{V_{NSR}} - J_{tr} \frac{V_{JSR}}{V_{NSR}},$$
(A92)

(A91)

$$\frac{d[\mathrm{Ca}^{2^{+}}]_{\mathrm{m}}}{dt} = \delta(V_{\mathrm{uni}} - V_{\mathrm{NaCa}}), \tag{A93}$$

$$\frac{d[\text{Na}^+]_i}{dt} = -(I_{\text{Na}} + I_{\text{Na,b}} + I_{\text{ns,Na}} + 3I_{\text{NaCa}} + 3I_{\text{NaK}}) \frac{A_{\text{cap}}}{V_{\text{myo}}F},$$
(A94)

$$\frac{d[K^{+}]_{i}}{dt} = -(I_{K} + I_{K_{1}} + I_{K_{p}} + I_{ns,K} + I_{Ca,K} - 2I_{NaK})\frac{A_{cap}}{V_{myo}F}.$$
(A95)

TABLE 11 Force generation parameters

Symbol	Value	Units	Description	Eq.	Refs.
k _{pn} ^{trop}	0.04	ms ⁻¹	Transition rate from tropomyosin permissive to nonpermissive.	A96	(15)
SL	2.15	μ m	Sarcomere length.	A111	(15)
$f_{\rm XB}$	0.05	ms ⁻¹	Transition rate from weak to strong crossbridge.	A102	*
$g_{\mathrm{XB}}^{\mathrm{min}}$	0.1	ms ⁻¹	Minimum transition rate from strong to weak crossbridge.	A105	*
ζ	0.1	$N~\mathrm{mm}^{-2}$	Conversion factor normalizing to physiological force.	A120	(15)
$V_{ m AM}^{ m max}$	7.2×10^{-3}	mM ms ⁻¹	Maximal rate of ATP hydrolysis by myofibrils (AM ATPase).	A122	†
$K_{\mathrm{M,AM}}^{\mathrm{ATP}}$	0.03	mM	ATP half-saturation constant of AM ATPase.	A122	(24)
$K_{i,AM}$	0.26	mM	ADP inhibition constant of AM ATPase.	A122	(24)

^{*}Adjusted from the value reported in Rice et al. (15) to reproduce the values of the developed force by ventricular guinea-pig muscles, as described in Ruf et al. (62).

Force generation model (15)

$$\frac{d[P_{o}]}{dt} = -(k_{pn}^{trop} + f_{01})[P_{o}] + k_{np}^{trop}[N_{o}] + g_{01}(SL)[P_{1}], \quad (A96)$$

$$\frac{d[P_{1}]}{dt} = -(k_{pn}^{trop} + f_{12} + g_{01}(SL))[P_{1}] + k_{np}^{trop}[N_{1}]$$

$$+ f_{01}[P_{0}] + g_{12}(SL)[P_{2}], \quad (A97)$$

TABLE 12 Cytoplasmic energy handling parameters

Symbol	Value	Units	Description	Eq.	Refs.
C_{T}	25	mM	Total concentration of creatine metabolites (both compartments).		(63,64)
$k_{\mathrm{CK}}^{\mathrm{cyto}}$	1.4×10^{-4}	ms^{-1}	Forward rate constant of cytoplasmic CK.	A140	*
$k_{\mathrm{CK}}^{\mathrm{mito}}$	1.33×10^{-6}	ms^{-1}	Forward rate constant of mitochondrial CK.	A141	*
$k_{\mathrm{tr}}^{\mathrm{Cr}}$	2.0×10^{-3}	ms ⁻¹	Transfer rate constant of CrP.	A142	*
$K_{\rm EQ}$	0.0095		Equilibrium constant of CK.	A140	(63) [†]
$V_{ m ATPase}^{ m cyto}$	$1.0 \ 10^{-5}$	mM ms ⁻¹	Constitutive cytosolic ATP consumption rate.	A125	‡

^{*}The forward rate constants of the CK reaction were adjusted to reproduce the range of values from Clark et al. (67).

[†]Estimated from Ebus and Stienen (30).

[†]The equilibrium constant was averaged from that reported by Selivanov et al. (62) and the one by Saupe et al. (66) including the proton concentration [H⁺] inside the equilibrium constant.

[‡]Calculated according to the 25% of the resting energy being used for macromolecular turnover as reported by Ingwall and Weiss (65).

TABLE 13 Tricarboxylic acid cycle parameters

Symbol	Value	Units	Description	Eq.	Refs.
[AcCoA]	1.0	mM	Acetyl CoA concentration.	A143	(16)
$k_{\text{cat}}^{\text{CS}}$	0.05	ms^{-1}	Catalytic constant of CS.	A143	*
$k_{\mathrm{cat}}^{\mathrm{CS}}$ $E_{\mathrm{T}}^{\mathrm{CS}}$	0.4	mM	Concentration of CS.	A143	(16)
$K_{\rm M}^{\rm AcCoA}$	1.26×10^{-2}	mM	Michaelis constant for AcCoA.	A143	(16)
$K_{\mathrm{M}}^{\mathrm{OAA}}$	6.4×10^{-4}	mM	Michaelis constant for OAA.	A143	(16)
C_{Kint}	1.0	mM	Sum of TCA cycle intermediates' concentration.	A138	(16)
$C_{ m Kint}$ $k_{ m f}^{ m ACO}$ $K_{ m E}^{ m ACO}$	1.25×10^{-2}	ms^{-1}	Forward rate constant of ACO.	A144	(16)
$K_{\rm E}^{ m ACO}$	2.22		Equilibrium constant of ACO.	A144	(16)
$K_{\mathrm{ADP}}^{\mathrm{a}}$	0.62	mM	Activation constant by ADP.	A145	†
K_{Ca}^{a}	0.0005	mM	Activation constant for Ca ²⁺ .	A145	†
Kinadh	0.19	mM	Inhibition constant by NADH.	A146	(16)
$k_{\rm cat}^{\rm IDH}$	0.03	ms^{-1}	Rate constant of IDH.	A147	*
k _{cat} ^{IDH} E _T	0.109	mM	Concentration of IDH.	A147	(16)
[H ⁺]	2.5×10^{-5}	mM	Matrix proton concentration.	A147	(16)
$k_{h,1}$	8.1×10^{-5}	mM	Ionization constant of IDH.	A147	(16)
$k_{\rm h,2}$	5.98×10^{-5}	mM	Ionization constant of IDH.	A147	(16)
$K_{\rm M}^{\rm ISOC}$	1.52	mM	Michaelis constant for isocitrate.	A147	(16)
N:	2.0		Cooperativity for isocitrate.	A147	(16)
K ^{NAD}	0.923	mM	Michaelis constant for NAD ⁺ .	A147	(16)
$K_{\mathrm{M}}^{\mathrm{NAD}}$ $K_{\mathrm{D}}^{\mathrm{Mg}^{2+}}$ $K_{\mathrm{D}}^{\mathrm{Ca}^{2+}}$	0.0308	mM	Activation constant for Mg ²⁺ .	A148	(16)
$K_{\rm C}^{\rm Ca^{2+}}$	1.27×10^{-3}	mM	Activation constant for Ca ²⁺ .	A148	(16)
EKGDH	0.5	mM	Concentration of KGDH.	A149	(16)
$E_{\mathrm{T}}^{\mathrm{K}\mathrm{GDH}}$ $E_{\mathrm{T}}^{\mathrm{K}\mathrm{GDH}}$ $k_{\mathrm{cat}}^{\mathrm{K}\mathrm{DGH}}$ $K_{\mathrm{M}}^{\mathrm{K}\mathrm{K}\mathrm{G}}$ $K_{\mathrm{M}}^{\mathrm{N}\mathrm{AD}}$	0.05	ms^{-1}	Rate constant of KGDH.	A149	*
καKG	1.94	mM	Michaelis constant for αKG .	A149	(16)
K ^{NAD}	38.7	mM	Michaelis constant for NAD.	A149	(16)
n	1.2	1111111	Hill coefficient of KGDH for αKG .	A149	(16)
$n_{\alpha { m KG}}$ ${ m Mg}^{2+}$	0.4	mM	Mg ²⁺ concentration in mitochondria.	A148	(16)
	5.0×10^{-4}	$\mathrm{mM}^{-1} \mathrm{ms}^{-1}$	Forward rate constant of SL.	A150	*
$k_{ m f}^{ m SL}$ $K_{ m E}^{ m SL}$	3.115	IIIIVI IIIS	Equilibrium constant of the SL reaction.	A150	(16)
(CoA)	0.02	mM	Coenzyme A concentration.	A150	(16)
	3.0×10^{-3}	ms ⁻¹	Rate constant of SDH.	A150	(10)
cat SDH					
ET VSuc	0.5	mM	SDH enzyme concentration.	A151	(16)
K _M	0.03	mM	Michaelis constant for succinate.	A151	(16)
Ki om	1.3	mM	Inhibition constant by fumarate.	A151	(16)
$\begin{array}{l} k_{\mathrm{cat}}^{\mathrm{SDH}} \\ k_{\mathrm{T}}^{\mathrm{SDH}} \\ K_{\mathrm{M}}^{\mathrm{Suc}} \\ K_{\mathrm{i}}^{\mathrm{FUM}} \\ K_{\mathrm{i},\mathrm{sdh}}^{\mathrm{OAA}} \\ k_{\mathrm{f}}^{\mathrm{FH}} \end{array}$	$0.15 \\ 3.32 \times 10^{-3}$	mM	Inhibition constant by oxalacetate.	A151	(16)
K _f ¹¹¹		ms^{-1}	Forward rate constant for FH.	A152	
$K_{\rm E}^{ m FH}$	1.0		Equilibrium constant of FH.	A152	(16)
$k_{\rm h1}$	1.13×10^{-5}	mM	Ionization constant of MDH.	A153	(16)
k_{h2}	26.7	mM	Ionization constant of MDH.	A153	(16)
$k_{\rm h3}$	6.68×10^{-9}	mM	Ionization constant of MDH.	A154	(16)
$k_{\rm h4}$	5.62×10^{-6}	mM	Ionization constant of MDH.	A154	(16)
k _{offset}	3.99×10^{-2}		pH-independent term in the pH activation factor of MDH.	A153	(16)
$k_{\mathrm{cat}}^{\mathrm{MDH}}$	0.111	ms^{-1}	Rate constant of MDH.	A155	*
$E_{\mathrm{T}}^{\mathrm{MDH}}$	0.154	mM	Total MDH enzyme concentration.	A155	(16)
$K_{ m M}^{ m MAL}$	1.493	mM	Michaelis constant for malate.	A155	(16)
$K_{\rm i}^{ m OAA}$ $K_{ m M}^{ m NAD}$	3.1×10^{-3}	mM	Inhibition constant for oxalacetate.	A155	(16)
$K_{ m M}^{ m NAD}$	0.2244	mM	Michaelis constant for NAD ⁺ .	A155	(16)
[GLU]	10.0	mM	Glutamate concentration.	A156	(16)
$k_{\mathrm{f}}^{\mathrm{AAT}}$	6.44×10^{-4}	ms^{-1}	Forward rate constant of AAT.	A156	(16)
$K_{\rm E}^{\rm AAT}$	6.6		Equilibrium constant of AAT.	A156	(16)
k_{ASP}	1.5×10^{-6}	ms^{-1}	Rate constant of aspartate consumption.	A156	*

^{*}The kinetic constants of all the TCA cycle enzyme steps have been multiplied by a factor of 1.5–4 with respect to those indicated in Cortassa et al. (16) to match the fluxes of the TCA cycle (68) in the integrated model that faces additional restrictions than those of the isolated mitochondrial model.

 $^{^{\}dagger}$ The values of the isocitrate dehydrogenase activation constants by ADP and Ca^{2+} have been modified to reproduce appropriately the kinetics reported by Rutter and Denton (68).

TABLE 14 Oxidative phosphorylation parameters

Symbol	Value	Units	Description	Eq.	Refs.
$r_{\rm a}$	6.394×10^{-13}	ms^{-1}	Sum of products of rate constants.	A157	(16)
$r_{\rm b}$	1.762×10^{-16}	ms^{-1}	Sum of products of rate constants.	A158	(16)
r_{c1}	2.656×10^{-22}	ms^{-1}	Sum of products of rate constants.	A157	(16)
r_{c2}	8.632×10^{-30}	ms^{-1}	Sum of products of rate constants.	A157	(16)
r_1	2.077×10^{-18}		Sum of products of rate constants.	A157	(16)
r_2	1.728×10^{-9}		Sum of products of rate constants.	A157	(16)
r_3	1.059×10^{-26}		Sum of products of rate constants.	A157	(16)
$ ho^{ m res}$	3.0×10^{-3}	mM	Concentration of electron carriers (respiratory complexes I-III-IV).	A157	(16)
K_{res}	1.35×10^{18}		Equilibrium constant of respiration.	A159	(16)
$\rho^{\text{res(F)}}$	3.75×10^{-4}	mM	Concentration of electron carriers (respiratory complexes II-III-IV).	A161	*
$\Delta\Psi_{ m B}$	50	mV	Phase boundary potential.	A157	(16)
G	0.85		Correction factor for voltage.	A157	(16)
$K_{\text{res(F)}}$	5.765×10^{13}		Equilibrium constant of FADH ₂ oxidation.	A162	(16)
[FADH2]	1.24	mM	Concentration of FADH ₂ (reduced).	A162	(16)
[FAD]	0.01	mM	Concentration of FAD (oxidized).	A162	(16)
p_{a}	1.656×10^{-8}	ms^{-1}	Sum of products of rate constants.	A163	(16)
p_{b}	3.373×10^{-10}	ms^{-1}	Sum of products of rate constants.	A164	(16)
p_{c1}	9.651×10^{-17}	ms^{-1}	Sum of products of rate constants.	A163	(16)
p_{c2}	4.585×10^{-17}	ms^{-1}	Sum of products of rate constants.	A163	(16)
p_1	1.346×10^{-8}		Sum of products of rate constants.	A163	(16)
p_2	7.739×10^{-7}		Sum of products of rate constants.	A163	(16)
p_3	6.65×10^{-15}		Sum of products of rate constants.	A163	(16)
$ ho_3^{ m F1}$	1.5	mM	Concentration of F_1F_0 -ATPase.	A163	(16)
K_{F1}	1.71×10^{6}		Equilibrium constant of ATP hydrolysis.	A165	(16)
Pi	2.0	mM	Inorganic phosphate concentration.	A165	†
C_{A}	1.5	mM	Total sum of mito adenine nucleotides.	A129	†
V_{maxANT}	0.025	$\mathrm{mM}~\mathrm{ms}^{-1}$	Maximal rate of the ANT.	A139	(16)
h^{ANT}	0.5		Fraction of $\Delta\Psi_{\rm m}$.	A139	(16)
g_{H}	1.0×10^{-8}	$\mathrm{mM}~\mathrm{ms}^{-1}~\mathrm{mV}^{-1}$	Ionic conductance of the inner membrane.	A166	(16)
Δ pH	-0.6	pH units	pH gradient across the inner membrane.	A167	(16)
C_{PN}	10.0	mM	Total sum of mito pyridine nucleotides.	A160	(16)
$C_{ m mito}$	1.812×10^{-3}	$ m mM~mV^{-1}$	Inner membrane capacitance.	A123	(16)

^{*}The respiratory complex II carriers concentration was adjusted with respect to the value in Cortassa et al. (16) to match the reported range of oxygen consumption rates (0.04–0.5 mM s⁻¹ = 5–60 μ Mol O₂/min/mg) (1).

$$\frac{d[P_2]}{dt} = -(f_{23} + g_{12}(SL))[P_2] + f_{12}[P_1] + g_{23}(SL)[P_3], (A98)$$

$$\frac{d[P_3]}{dt} = -g_{23}(SL)[P_3] + f_{23}[P_2], \tag{A99}$$

$$\frac{d[N_1]}{dt} = k_{pn}^{trop}[P_1] + (k_{np}^{trop} + g'_{01}(SL))[N_1],$$
 (A100)

$$[N_0] = 1 - ([N_1] + [P_0] + [P_1] + [P_2] + [P_3]),$$
 (A101)

$$f_{01} = 3 \times f_{XB},$$
 (A102)

$$f_{12} = 10 \times f_{XB},$$
 (A103)

$$f_{23} = 7 \times f_{XB},$$
 (A104)

$$g_{01} = 1 \times g_{XB}^{\min}, \tag{A105}$$

$$g_{12} = 2 \times g_{XB}^{min},$$
 (A106)

$$g_{23} = 3 \times g_{XB}^{min},$$
 (A107)

$$g_{01}(SL) = 1 \times \phi \times g_{XB}^{\min}, \tag{A108}$$

$$g_{12}(SL) = 2 \times \phi \times g_{yg}^{min},$$
 (A109)

$$g_{23}(SL) = 3 \times \phi \times g_{\text{NR}}^{\text{min}}, \tag{A110}$$

$$\phi = 1 + \frac{2.3 - SL}{(2.3 - 1.7)^{1.6}},$$
(A111)

$$k_{\rm np}^{\rm trop} = k_{\rm pn}^{\rm trop} \left[\frac{[\rm LTRPNCa]}{K_{1/2}^{\rm trop} [\rm LTRPN]_{\rm tot}} \right]^{\rm N^{\rm trop}},$$
 (A112)

$$K_{1/2}^{\text{trop}} = \left(1 + \frac{K_{\text{Ca}}^{\text{trop}}}{1.710^{-3} - 0.810^{-3} \frac{(SL - 1.7)}{0.6}}\right)^{-1}, \quad (A113)$$

$$N^{\text{trop}} = 3.5 \times SL - 2.0,$$
 (A114)

$$K_{\text{Ca}}^{\text{trop}} = \frac{k_{\text{ltrpn}}^{-}}{k_{\text{ltrpn}}^{+}},\tag{A115}$$

[†]The total nucleotide level and inorganic phosphate were corrected with respect to previous publication (16) to follow reported experimental evidence (1,69).

TABLE 15 Mitochondrial Ca²⁺ handling parameters

Symbol	Value	Units	Description	Eq.	Refs.
$V_{ m max}^{ m uni}$	0.0275	mM ms ⁻¹	V_{max} uniporter Ca^{2+} transport.	A168	*
$\Delta\Psi^{\circ}$	91	mV	Offset membrane potential.	A168	(16)
$K_{\rm act}$	3.8×10^{-4}	mM	Activation constant.	A168	(16)
$K_{\rm trans}$	0.019	mM	$K_{\rm d}$ for translocated Ca^{2+} .	A168	(16)
L	110.0		$K_{\rm eq}$ for conformational transitions in uniporter.	A168	(16)
$n_{\rm a}$	2.8		Uniporter activation cooperativity.	A168	(16)
$V_{ m max}^{ m NaCa}$	1.0×10^{-4}	mM ms ⁻¹	V _{max} of Na ⁺ /Ca ²⁺ antiporter.	A169	(16)
b	0.5		$\Delta \Psi_{\rm m}$ dependence of Na ⁺ /Ca ²⁺ antiporter.	A169	(16)
K_{Na}	9.4	mM	Antiporter Na ⁺ constant.	A169	(16)
K_{Ca}	3.75×10^{-4}	mM	Antiporter Ca ²⁺ constant.	A169	(16)
n	3		Na ⁺ /Ca ²⁺ antiporter cooperativity.	A169	(16)
δ	$3.0 \ 10^{-4}$		Fraction of free [Ca ²⁺] _m .	A93	(16)

^{*}The maximal rate of the Ca²⁺ uniporter had to be adjusted to meet the transport fluxes experimentally determined (70,71) in the new integrated model structure in which the Ca²⁺ levels in the cytoplasm are no longer steady as they were in the isolated mitochondrial model (16).

$$\sum PATHS = g_{01} g_{12} g_{23} + f_{01} g_{12} g_{23} + f_{01} f_{12} g_{23} + f_{01} f_{12} f_{23},$$
(A116)

$$P_{1_{\text{max}}} = \frac{f_{01} g_{12} g_{23}}{\sum PATHS},$$
 (A117)

$$P_{2_{\text{max}}} = \frac{f_{01} f_{12} g_{23}}{\sum PATHS},$$
 (A118)

$$P_{3_{\text{max}}} = \frac{f_{01}f_{12}f_{23}}{\sum PATHS},$$
 (A119)

Force =
$$\zeta \frac{P_1 + N_1 + 2P_2 + 3P_3}{P_{1,\dots,} + 2P_{2,\dots,} + 3P_{3,\dots,}}$$
, (A120)

$$Force_{Norm} = \frac{P_1 + N_1 + P_2 + P_3}{P_{1_{\max}} + P_{2_{\max}} + P_{3_{\max}}},$$
 (A121)

$$V_{\text{AM}} = V_{\text{AM}}^{\text{max}} \left(\frac{f_{01} \left[\mathbf{P}_{0} \right] + f_{12} \left[\mathbf{P}_{1} \right] + f_{23} \left[\mathbf{P}_{2} \right]}{f_{01} + f_{12} + f_{23}} \right) \times \left(1 + \frac{K_{\text{M,AM}}^{\text{ATP}}}{\left[\text{ATP} \right]_{i}} \left[1 + \frac{\left[\text{ADP} \right]_{i}}{K_{i,\text{AM}}} \right] \right)^{1}.$$
 (A122)

See Table 11.

Mitochondrial membrane potential ($\Delta \Psi_m$)

$$\frac{d\Delta\Psi_{\rm m}}{dt} = \frac{V_{\rm He} + V_{\rm He(F)} - V_{\rm Hu} - V_{\rm ANT} - V_{\rm HLeak} - V_{\rm NaCa} - 2\,V_{\rm uni}}{C_{\rm mito}}. \tag{A123}$$

Energy metabolites

$$\begin{split} \frac{d[\text{ATP}]_{\text{i}}}{dt} &= V_{\text{ANT}} \frac{V_{\text{mito}}}{V_{\text{myo}}} - V_{\text{CK}}^{\text{mito}} - V_{\text{AM}} - \frac{1}{2} J_{\text{up}} \\ &- (I_{\text{pCa}} + I_{\text{NaK}}) \frac{A_{\text{cap}}}{V_{\text{myo}} F}, \end{split} \tag{A124}$$

$$\frac{d[\text{ATP}]_{ic}}{dt} = -V_{\text{CK}}^{\text{cyto}} - V_{\text{ATPase}}^{\text{cyto}}, \tag{A125}$$

$$\frac{d[\text{CrP}]_{i}}{dt} = V_{\text{CK}}^{\text{mito}} - V_{\text{tr}}^{\text{CrP}}, \tag{A126}$$

$$\frac{d[\text{CrP}]_{\text{ic}}}{dt} = V_{\text{tr}}^{\text{CrP}} + V_{\text{CK}}^{\text{cyto}}, \tag{A127}$$

$$\frac{d[ADP]_{m}}{dt} = V_{ANT} - V_{ATPase} - V_{SL}, \tag{A128}$$

$$[ATP]_{m} = C_{A} - [ADP]_{m}, \qquad (A129)$$

$$\frac{d[\text{NADH}]}{dt} = -V_{02} + V_{\text{IDH}} + V_{\text{KGDH}} + V_{\text{MDH}}, \quad (A130)$$

$$\frac{d[\text{ISOC}]}{dt} = V_{\text{ACO}} - V_{\text{IDH}}, \tag{A131}$$

$$\frac{d[\alpha \text{KG}]}{dt} = V_{\text{IDH}} - V_{\text{KGDH}} + V_{\text{AAT}}, \tag{A132}$$

$$\frac{d[SCoA]}{dt} = V_{KGDH} - V_{SL}, \tag{A133}$$

$$\frac{d[Suc]}{dt} = V_{SL} - V_{SDH}, \tag{A134}$$

$$\frac{d[\text{FUM}]}{dt} = V_{\text{SDH}} - V_{\text{FH}},\tag{A135}$$

$$\frac{d[\text{MAL}]}{dt} = V_{\text{FH}} - V_{\text{MDH}},\tag{A136}$$

$$\frac{d[\text{OAA}]}{dt} = V_{\text{MDH}} - V_{\text{CS}} - V_{\text{AAT}}, \tag{A137}$$

$$[CIT] = C_{Kint} - ([ISOC] + [\alpha KG] + [SCoA] + [Suc]$$
$$+ [FUM] + [MAL] + [OAA]).$$
(A138)

Energy metabolism reaction rates

Cytosolic reaction rates

$$f_{\rm a}^{\rm KGDH} = \left[\left(1 + \frac{[{\rm Mg}^{2^+}]}{K_{\rm D}^{{\rm Mg}^{2^+}}} \right) \left(1 + \frac{[{\rm Ca}^{2^+}]_{\rm m}}{K_{\rm D}^{{\rm Ca}^{2^+}}} \right) \right]^{-1}, \quad (A148)$$

$$V_{\text{ANT}} = V_{\text{maxANT}} \frac{0.75 \left(1 - \frac{0.25 \left[\text{ATP}\right]_{\text{i}} \times 0.45 \left[\text{ADP}\right]_{\text{m}}}{0.17 \left[\text{ADP}\right]_{\text{i}} \times 0.025 \left[\text{ATP}\right]_{\text{m}}}\right) \left(e^{-\frac{F}{RT}\Delta\Psi_{\text{m}}}\right)}{\left(1 + \frac{0.25 \left[\text{ATP}\right]_{\text{i}}}{0.225 \left[\text{ADP}\right]_{\text{i}}} e^{\left(\frac{-h^{\text{ANT}} F \Delta \Psi_{\text{m}}}{RT}\right)\right) \left(1 + \frac{0.45 \left[\text{ADP}\right]_{\text{m}}}{0.025 \left[\text{ATP}\right]_{\text{m}}}\right)},$$
(A139)

$$V_{\text{CK}}^{\text{cyto}} = k_{\text{CK}}^{\text{cyto}} \left([\text{ATP}]_{\text{ic}} \left[\text{Cr} \right]_{\text{ic}} - \frac{[\text{ADP}]_{\text{ic}} \left[\text{CrP} \right]_{\text{ic}}}{K_{\text{EQ}}} \right), \quad (\text{A140})$$

$$V_{\text{CK}}^{\text{mito}} = k_{\text{CK}}^{\text{mito}} \left(\left[\text{ATP} \right]_{i} \left[\text{Cr} \right]_{i} - \frac{\left[\text{ADP} \right]_{i} \left[\text{CrP} \right]_{i}}{K_{\text{FO}}} \right), \quad (A141)$$

$$V_{\text{tr}}^{\text{CrP}} = k_{\text{tr}}^{\text{Cr}}([\text{CrP}]_{\text{i}} - [\text{CrP}]_{\text{ic}}).$$
 (A142)

See Table 12.

Tricarboxylic acid cycle reaction rates

$$V_{\text{CS}} = k_{\text{cat}}^{\text{CS}} E_{\text{T}}^{\text{CS}} \left(1 + \frac{K_{\text{M}}^{\text{AcCoA}}}{[\text{AcCoA}]} + \frac{K_{\text{M}}^{\text{OAA}}}{[\text{OAA}]} + \frac{K_{\text{M}}^{\text{OAA}}}{[\text{OAA}]} + \frac{K_{\text{M}}^{\text{OAA}}}{[\text{AcCoA}]} + \frac{K_{\text{M}}^{\text{OAA}}}{[\text{OAA}]} \right)^{-1},$$
(A143)

$$V_{\text{ACO}} = k_{\text{f}}^{\text{ACO}} \left([\text{CIT}] - \frac{[\text{ISOC}]}{K_{\text{F}}^{\text{ACO}}} \right),$$
 (A144)

$$f_{\rm a}^{\rm IDH} = \left[\left(1 + \frac{[{\rm ADP}]_{\rm m}}{K_{\rm ADP}^{\rm a}} \right) \left(1 + \frac{[{\rm Ca}^{2^+}]_{\rm m}}{K_{\rm Ca}^{\rm a}} \right) \right]^{-1},$$
 (A145)

$$V_{\text{KGDH}} = \frac{k_{\text{cat}}^{\text{KGDH}} E_{\text{T}}^{\text{KGDH}}}{1 + f_{\text{a}}^{\text{KGDH}} \left(\frac{K_{\text{M}}^{\alpha \text{KG}}}{[\alpha \text{KG}]}\right)^{n_{\text{a}\text{KG}}} + f_{\text{a}}^{\text{KGDH}} \frac{K_{\text{M}}^{\text{NAD}}}{[\text{NAD}]}}, \quad (A149)$$

$$V_{\rm SL} = k_{\rm f}^{\rm SL} \left([{\rm SCoA}] [{\rm ADP}]_{\rm m} - \frac{[{\rm Suc}] [{\rm ATP}]_{\rm m} [{\rm CoA}]}{K_{\rm E}^{\rm SL}} \right), (A150)$$

$$V_{\text{SDH}} = \frac{k_{\text{cat}}^{\text{SDH}} E_{\text{T}}^{\text{SDH}}}{1 + \left(\frac{K_{\text{M}}^{\text{Suc}}}{[\text{Suc}]}\right) \left(1 + \frac{[\text{OAA}]}{K_{\text{i,sdh}}^{\text{OAA}}}\right) \left(1 + \frac{[\text{FUM}]}{K_{\text{i}}^{\text{FUM}}}\right)}, \text{ (A151)}$$

$$V_{\rm FH} = {\rm k_f^{FH}} \bigg({\rm [FUM]} - \frac{{\rm [MAL]}}{K_{\rm F}^{\rm FH}} \bigg),$$
 (A152)

$$f_{\text{h,a}} = \left(1 + \frac{[\text{H}^+]}{k_{\text{h1}}} + \frac{[\text{H}^+]^2}{k_{\text{h1}}k_{\text{h2}}}\right)^{-1} + k_{\text{offset}},$$
 (A153)

$$f_{\text{h,i}} = \left(1 + \frac{k_{\text{h3}}}{[\text{H}^+]} + \frac{k_{\text{h3}} k_{\text{h4}}}{[\text{H}^+]^2}\right)^{-2},$$
 (A154)

$$V_{\text{MDH}} = \frac{k_{\text{cat}}^{\text{MDH}} E_{\text{T}}^{\text{MDH}} f_{\text{h,a}} f_{\text{h,i}}}{1 + \frac{K_{\text{M}}^{\text{MAL}}}{[\text{MAL}]} \left(1 + \frac{[\text{OAA}]}{K_{i}^{\text{OAA}}}\right) + \frac{K_{\text{M}}^{\text{NAD}}}{[\text{NAD}]} + \frac{K_{\text{M}}^{\text{MAL}}}{[\text{MAL}]} \left(1 + \frac{[\text{OAA}]}{K_{i}^{\text{OAA}}}\right) \frac{K_{\text{M}}^{\text{NAD}}}{[\text{NAD}]},$$
(A155)

$$f_{i}^{\text{IDH}} = \left(1 + \frac{[\text{NADH}]}{K_{i,\text{NADH}}}\right), \qquad (\text{A146})$$

$$V_{\text{IDH}} = k_{\text{cat}}^{\text{IDH}} E_{\text{T}}^{\text{IDH}} \left[\left(1 + \frac{[\text{H}^{+}]}{k_{\text{h},1}} + \frac{k_{\text{h},2}}{[\text{H}^{+}]}\right) + f_{i}^{\text{IDH}} \left(\frac{K_{\text{M}}^{\text{NAD}}}{[\text{NAD}]}\right) \right]^{-1}, \qquad (\text{A147})$$

$$+ f_{a}^{\text{IDH}} \left(\frac{K_{\text{M}}^{\text{ISOC}}}{[\text{ISOC}]}\right)^{\text{ni}} + f_{a}^{\text{IDH}} f_{i}^{\text{IDH}} \left(\frac{K_{\text{M}}^{\text{ISOC}}}{[\text{ISOC}]}\right)^{\text{ni}} \left(\frac{K_{\text{M}}^{\text{NAD}}}{[\text{NAD}]}\right)^{-1}, \qquad (\text{A147}) \qquad \text{See Table 13}.$$

Oxidative phosphorylation reaction rates

$$\Delta \mu_{\rm H} = -2.303 \frac{RT}{F} \Delta p H + \Delta \Psi_{\rm m}. \tag{A167}$$

$$V_{\rm O_2} = 0.5 \, \rho^{\rm res} \frac{\left(r_{\rm a} + r_{\rm cl} \, e^{\left(\frac{6 \rm F}{\rm A} \Psi_{\rm B}}{\rm RT}\right)}\right) e^{\left(\frac{\Lambda_{\rm res} \, F}{\rm RT}\right)} - r_{\rm a} \, e^{\left(\frac{g \, 6 \, F}{\rm A} \mu_{\rm H}}\right)} + r_{\rm c2} \, e^{\left(\frac{\Lambda_{\rm res} \, F}{\rm RT}\right)} \, e^{\left(\frac{g \, 6 \, F}{\rm A} \mu_{\rm H}}\right)}}{\left(1 + r_{\rm l} \, e^{\left(\frac{F}{\rm A} \mu_{\rm res}\right)}\right) e^{\left(\frac{6 \, F}{\rm A} \Psi_{\rm B}}\right)} + \left(r_{\rm 2} + r_{\rm 3} \, e^{\left(\frac{F}{\rm A} \mu_{\rm res}\right)}\right) e^{\left(\frac{g \, 6 \, F}{\rm A} \mu_{\rm H}}\right)}}, \tag{A157}$$

 $V_{\mathrm{He}} =$

$$6\rho^{\text{res}} \frac{\left(r_{\text{a}}e^{\left(\frac{\Lambda_{\text{Pes}}F}{RT}\right)} - \left(r_{\text{a}} + r_{\text{b}}\right)e^{\left(\frac{6F\Delta\mu_{\text{H}}}{RT}\right)}\right)}{\left(1 + r_{1}e^{\left(\frac{F\Lambda_{\text{res}}}{RT}\right)}\right)e^{\left(\frac{6F\Delta\Psi_{\text{R}}}{RT}\right)} + \left(r_{2} + r_{3}e^{\left(\frac{F\Lambda_{\text{res}}}{RT}\right)}\right)e^{\left(\frac{6F\Delta\mu_{\text{H}}}{RT}\right)}}, \qquad V_{\text{uni}} = \\ (A158) \qquad \qquad \frac{\left[\text{Ca}^{2+}\right]_{\text{i}}}{V}\left(1 + \frac{\left[\text{Ca}^{2+}\right]_{\text{i}}}{V}\right)}$$

$$r_1 e^{\left(\frac{\text{FA}_{\text{RES}}}{\text{RT}}\right)} e^{\left(\frac{\text{oraw}_{\text{RT}}}{\text{RT}}\right)} + \left(r_2 + r_3 e^{\left(\frac{\text{FA}_{\text{RES}}}{\text{RT}}\right)}\right) e^{\left(\frac{\text{goraw}_{\text{RT}}}{\text{RT}}\right)}$$
(A158)

$$A_{\text{res}} = \frac{RT}{F} \ln \left(K_{\text{res}} \sqrt{\frac{[\text{NADH}]}{[\text{NAD}^+]}} \right), \tag{A159}$$

(A158)
$$V_{\text{max}}^{\text{uni}} \frac{\frac{\left[\text{Ca}^{2+}\right]_{i}}{K_{\text{trans}}} \left(1 + \frac{\left[\text{Ca}^{2+}\right]_{i}}{K_{\text{trans}}}\right)^{3} \frac{2F(\Delta \Psi_{\text{m}} - \Delta \Psi^{o})}{RT}}{RT},$$

$$A_{\text{res}} = \frac{RT}{F} \ln \left(K_{\text{res}} \sqrt{\frac{\left[\text{NADH}\right]}{\left[\text{NAD}^{+}\right]}}\right), \qquad (A159) \frac{\left(1 + \frac{\left[\text{Ca}^{2+}\right]_{i}}{K_{\text{trans}}}\right)^{4} + \frac{L}{\left(1 + \frac{\left[\text{Ca}^{2+}\right]_{i}}{K_{\text{act}}}\right)^{n_{\text{a}}}} \left(1 - e^{\left(\frac{-2F(\Delta \Psi_{\text{m}} - \Delta \Psi^{o})}{RT}\right)}\right),$$

$$[\text{NAD}^{+}] = C_{\text{PN}} - [\text{NADH}], \qquad (A160)$$

$$(A168)$$

$$V_{\mathrm{He}(\mathrm{F})} = 4 \, \rho^{\mathrm{res}(\mathrm{F})} \frac{\left(r_{\mathrm{a}} \, e^{\left(\frac{\Lambda_{\mathrm{res}(\mathrm{F})}^{\mathrm{F}}}{\mathrm{RT}}\right)} - (r_{\mathrm{a}} + r_{\mathrm{b}}) \, e^{\left(\frac{\mathrm{g} \, 6\mathrm{F} \, \Delta \mu_{\mathrm{H}}}{\mathrm{RT}}\right)}\right)}{\left(1 + r_{\mathrm{1}} \, e^{\left(\frac{\mathrm{F} \, \Lambda_{\mathrm{res}(\mathrm{F})}}{\mathrm{RT}}\right)}\right) e^{\left(\frac{6\, \mathrm{F} \, \Delta \Psi_{\mathrm{B}}}{\mathrm{RT}}\right)} + \left(r_{\mathrm{2}} + r_{\mathrm{3}} \, e^{\left(\frac{\mathrm{F} \, \Lambda_{\mathrm{res}(\mathrm{F})}}{\mathrm{RT}}\right)}\right) e^{\left(\frac{\mathrm{g} \, 6\mathrm{F} \, \Delta \mu_{\mathrm{H}}}{\mathrm{RT}}\right)}}, \tag{A161}$$

$$A_{\text{res}(F)} = \frac{RT}{F} \ln \left(K_{\text{res}(F)} \sqrt{\frac{[\text{FADH}_2]}{[\text{FAD}]}} \right), \tag{A162}$$

$$V_{\text{NaCa}} = V_{\text{max}}^{\text{NaCa}} \frac{e^{\left(\frac{bF(\Delta \Psi_{\text{m}} - \Delta \Psi^{\circ}}{RT})}\right)} e^{\left(\ln \frac{[\text{Ca}^{2+}]_{\text{im}}}{[\text{Ca}^{2+}]_{\text{i}}}\right)}}{\left(1 + \frac{K_{\text{Na}}}{[\text{Na}_{\text{i}}^{+}]}\right)^{n} \left(1 + \frac{K_{\text{Ca}}}{[\text{Ca}^{2+}]_{\text{m}}}\right)}. \tag{A169}$$

$$V_{\text{ATPase}} = -\rho^{\text{FI}} \frac{\left(10^{2} p_{\text{a}} + p_{\text{c1}} e^{\left(\frac{3\text{F}\Delta\Psi_{\text{E}}}{\text{RT}}\right)}\right) e^{\left(\frac{\Lambda_{\text{FI}} \text{F}}{\text{RT}}\right)} - \left(p_{\text{a}} e^{\left(\frac{3\text{F}\Delta\mu_{\text{H}}}{\text{RT}}\right)} + p_{\text{c2}} e^{\left(\frac{\Lambda_{\text{FI}} \text{F}}{\text{RT}}\right)} e^{\left(\frac{3\text{F}\Delta\mu_{\text{H}}}{\text{RT}}\right)}\right)}{\left(1 + p_{\text{I}} e^{\left(\frac{\text{F}\Delta\mu_{\text{I}}}{\text{RT}}\right)}\right) e^{\left(\frac{3\text{F}\Delta\mu_{\text{B}}}{\text{RT}}\right)} + \left(p_{\text{2}} + p_{\text{3}} e^{\left(\frac{\text{F}\Delta\mu_{\text{I}}}{\text{RT}}\right)}\right) e^{\left(\frac{3\text{F}\Delta\mu_{\text{H}}}{\text{RT}}\right)}},$$
(A163)

 $-3\rho^{\rm Fl} \frac{10^2 p_{\rm a} \left(1 + e^{\left(\frac{{\rm Fr}_{\rm Fl}}{{\rm RT}}\right)}\right) - (p_{\rm a} + p_{\rm b}) e^{\left(\frac{{\rm Fr}_{\rm Fl}}{{\rm RT}}\right)}}{\left(1 + p_{\rm l} e^{\left(\frac{{\rm Fr}_{\rm Fl}}{{\rm RT}}\right)}\right) e^{\left(\frac{{\rm 3F}\Delta \mu_{\rm H}}{{\rm RT}}\right)} + \left(p_{\rm 2} + p_{\rm 3} e^{\left(\frac{{\rm Fr}_{\rm Fl}}{{\rm RT}}\right)}\right) e^{\left(\frac{{\rm 3F}\Delta \mu_{\rm H}}{{\rm RT}}\right)}},$ (A164)

$$A_{\rm FI} = \frac{RT}{F} \ln \left(K_{\rm FI} \frac{[\rm ATP]_{\rm m}}{[\rm ADP] \ Pi} \right), \tag{A165}$$

$$V_{\text{Hleak}} = g_{\text{H}} \Delta \mu_{\text{H}}, \tag{A166}$$

See Tables 15 and 16.

SUPPLEMENTARY MATERIAL

An online supplement to this article can be found by visiting BJ Online at http://www.biophysj.org.

The authors are grateful to Dr. Linda B. Stull and Michelle Leppo for their help with the rat trabeculae experiments.

This work was supported by grants from Falk Medical Trust No. P020032 (R.L.W.), National Institutes of Health No. R37HL54598 (B.O'R.), and No. P01HL081427 (B.O'R., R.L.W., E.M.).

TABLE 16 States' variables initial values

m_{Na} Sodium of n_{Na} Sodium of j_{Na} Intracellut $[\mathrm{Ca}^{+}]_{\mathrm{i}}$ Intracellut $[\mathrm{Ca}^{2+}]_{\mathrm{i}}$ Intracellut $[\mathrm{Ca}^{2+}]_{\mathrm{NSR}}$ Network $[\mathrm{Ca}^{2+}]_{\mathrm{ISR}}$ Junctional $[\mathrm{Ca}^{2+}]_{\mathrm{SS}}$ Ca $^{2+}$ con $[\mathrm{Ca}^{2+}]_{\mathrm{m}}$ Mitochom	mal membrane potential. channel activation gate. channel slow inactivation gate. In channel activation gate. In channel activation gate. Ilar Na ⁺ concentration. Ilar Ca ²⁺ concentration. Il SR Ca ²⁺ concentration. Il SR Ca ²⁺ concentration. Il SR Ca ²⁺ concentration. Il securitation in the subspace. In channel activation gate.	$ \begin{array}{r} -84.78 \\ 0.03282 \\ 0.98415 \\ 0.99003 \\ 1.616 \times 10^{-4} \\ 7.001 \\ 138.3 \\ 5.52 \times 10^{-5} \\ 0.1998 \\ 0.1998 \end{array} $
m_{Na} Sodium of n_{Na} Potassium [Na $^{+}$] _i Intracellu [Ca $^{2+}$] _i Intracellu [Ca $^{2+}$] _i Network [Ca $^{2+}$] _{jSR} Network Junctiona [Ca $^{2+}$] _{jSR} Junctiona [Ca $^{2+}$] _{jSR} Ga $^{2+}$ con [Ca $^{2+}$] _m Mitochon	channel activation gate. channel inactivation gate. channel slow inactivation gate. n channel activation gate. lar Na ⁺ concentration. lar K ⁺ concentration. lar Ca ²⁺ concentration. SR Ca ²⁺ concentration. l SR Ca ²⁺ concentration. centration in the subspace.	0.03282 0.98415 0.99003 1.616×10^{-4} 7.001 138.3 5.52×10^{-5} 0.1998 0.1998
n_{Na} Sodium of j_{Na} Sodium of j_{Na} Sodium of j_{Na} Sodium of j_{Na} Potassium [Na $^{+}$] _i Intracellu [Ca $^{2+}$] _i Intracellu [Ca $^{2+}$] _i Intracellu [Ca $^{2+}$] _i Network [Ca $^{2+}$] _{jSR} Junctiona [Ca $^{2+}$] _{jSR} Ca $^{2+}$ con [Ca $^{2+}$] _m Mitochon	channel inactivation gate. channel slow inactivation gate. n channel activation gate. lar Na ⁺ concentration. lar K ⁺ concentration. lar Ca ²⁺ concentration. SR Ca ²⁺ concentration. l SR Ca ²⁺ concentration. centration in the subspace.	0.98415 0.99003 1.616×10^{-4} 7.001 138.3 5.52×10^{-5} 0.1998 0.1998
j_{Na} Sodium of X Potassium j_{Na} Potassium j_{Na} Intracellu j_{Na} Intracellu j_{Na} Intracellu j_{Na} Network j_{Na} Network j_{Na} Unctional j_{Na} j_{Na} Unctional j_{Na}	channel slow inactivation gate. In channel activation gate. Ilar Na ⁺ concentration. Ilar K ⁺ concentration. Ilar Ca ²⁺ concentration.	0.99003 1.616×10^{-4} 7.001 138.3 5.52×10^{-5} 0.1998 0.1998
$\begin{array}{lll} X & & \text{Potassiur} \\ [\text{Na}^+]_i & & \text{Intracellu} \\ [\text{K}^+]_i & & \text{Intracellu} \\ [\text{Ca}^{2+}]_i & & \text{Intracellu} \\ [\text{Ca}^{2+}]_{\text{NSR}} & & \text{Network} \\ [\text{Ca}^{2+}]_{\text{JSR}} & & \text{Junctiona} \\ [\text{Ca}^{2+}]_{\text{SS}} & & \text{Ca}^{2+} \text{ coi} \\ [\text{Ca}^{2+}]_m & & \text{Mitochoi} \end{array}$	n channel activation gate. lar Na ⁺ concentration. lar K ⁺ concentration. lar Ca ²⁺ concentration. SR Ca ²⁺ concentration. l SR Ca ²⁺ concentration. centration in the subspace.	1.616×10^{-4} 7.001 138.3 5.52×10^{-5} 0.1998 0.1998
$\begin{array}{ll} [Na^+]_i & Intracellu \\ [K^+]_i & Intracellu \\ [Ca^{2^+}]_i & Intracellu \\ [Ca^{2^+}]_{NSR} & Network \\ [Ca^{2^+}]_{JSR} & Junctiona \\ [Ca^{2^+}]_{SS} & Ca^{2^+} & colling \\ [Ca^{2^+}]_m & Mitocholl$	lar Na ⁺ concentration. lar K ⁺ concentration. lar Ca ²⁺ concentration. SR Ca ²⁺ concentration. l SR Ca ²⁺ concentration. decentration in the subspace.	7.001 138.3 5.52×10^{-5} 0.1998 0.1998
$ \begin{array}{ll} [K^+]_i & Intracellu \\ [Ca^{2^+}]_i & Intracellu \\ [Ca^{2^+}]_{NSR} & Network \\ [Ca^{2^+}]_{JSR} & Junctiona \\ [Ca^{2^+}]_{SS} & Ca^{2^+} & colling \\ [Ca^{2^+}]_m & Mitocholl$	lar K ⁺ concentration. lar Ca ²⁺ concentration. SR Ca ²⁺ concentration. l SR Ca ²⁺ concentration. accentration in the subspace.	$ \begin{array}{c} 138.3 \\ 5.52 \times 10^{-5} \\ 0.1998 \\ 0.1998 \end{array} $
$ \begin{array}{lll} [Ca^{2^+}]_i & Intracellu \\ [Ca^{2^+}]_{NSR} & Network \\ [Ca^{2^+}]_{JSR} & Junctiona \\ [Ca^{2^+}]_{SS} & Ca^{2^+} & coi \\ [Ca^{2^+}]_m & Mitochoi \end{array} $	lar Ca ²⁺ concentration. SR Ca ²⁺ concentration. I SR Ca ²⁺ concentration. I centration in the subspace.	5.52×10^{-5} 0.1998 0.1998
$[Ca^{2+}]_{JSR}$ Junctiona $[Ca^{2+}]_{SS}$ Ca^{2+} con $[Ca^{2+}]_{m}$ Mitochon	of SR Ca ²⁺ concentration.	0.1998 0.1998
$[Ca^{2+}]_{JSR}$ Junctiona $[Ca^{2+}]_{SS}$ Ca^{2+} con $[Ca^{2+}]_{m}$ Mitochon	of SR Ca ²⁺ concentration.	0.1998
$[Ca^{2+}]_{SS}$ Ca^{2+} cor $[Ca^{2+}]_m$ Mitochor	centration in the subspace.	
[Ca ²⁺] _m Mitochor	icentration in the subspace.	= 0 = = · · · · 0 = 5
	dried from Coff concentration	5.857×10^{-5}
P Fraction		9.76×10^{-5}
	of RyR channels in P _{C1} state.	0.9299
	of RyR channels in P_{C2} state.	0.0700
	of RyR channels in P _{O2} state.	3.51×10^{-11}
	of RyR channels in P _{O1} state.	8.309×10^{-5}
C_0 L-type C	a ²⁺ channel	0.9991
closed	-mode normal.	
C_1 L-type C	a ²⁺ channel	8.175×10^{-5}
closed	-mode normal.	
C ₂ L-type C	a ²⁺ channel	2.508×10^{-9}
	-mode normal.	2.000 10
	a ²⁺ channel	3.421×10^{-14}
	-mode normal.	3.421 × 10
C_4 L-type C	a ²⁺ channel	1.749×10^{-19}
C ₄ L-type C	-mode normal.	1.749 \ 10
	a ²⁺ channel	2.624×10^{-20}
		2.024 × 10
	node normal.	0.00 \ 10=4
C_{Ca0} L-type C	a ²⁺ channel closed-mode Ca.	8.28×10^{-4}
C_{Cal} L-type C	a ²⁺ channel closed-mode Ca.	2.71×10^{-7}
C_{Ca2} L-type C	a ²⁺ channel closed-mode Ca.	3.326×10^{-11}
C_{Ca3} L-type C	a ²⁺ channel closed-mode Ca. a ²⁺ channel closed-mode Ca.	1.815×10^{-15}
C_{Ca4} L-type C	a ²⁺ channel closed-mode Ca.	3.712×10^{-20}
	a ²⁺ channel open-mode Ca.	0
Y ICa inact	ivation gate.	0.979
[LTRPNCa] Ca ²⁺ box	and to low-affinity	0.00849
tropon	in sites.	
[HTRPNCa] Ca ²⁺ box	and to high-affinity	0.1321
	in sites.	
	issive tropomyosin with	0.9998
	ossbridges.	******
	issive tropomyosin with	2.243×10^{-5}
	ossbridge.	2.243 × 10
		2.601 × 10 ⁻⁵
	ve tropomyosin with	2.601×10^{-5}
	ossbridges.	2 2 4 2 4 2 - 5
	ve tropomyosin with	2.248×10^{-5}
	ossbridge.	-
	ve tropomyosin with	4.199×10^{-5}
two cr	ossbridges.	_
[P ₃] Permissiv	e tropomyosin with	3.657×10^{-5}
three o	rossbridges.	
[ATP] _i EC coup	ing linked ATP concentration.	7.977
	ling linked ADP concentration.	0.023
	ATP concentration not	7.972
	to EC coupling.	
	ADP concentration not	0.028
		0.020
	to EC coupling.	10 207
	idrial linked creatine	18.297
	nate concentration.	40.00
	creatine phosphate	18.291
concer	tration.	
		(Continued)
		(Солинией)

Table 16 (Continued)

Symbol	Description	Value
[ADP] _m	Mitochondrial ADP concentration.	0.276
[NADH]	Mitochondrial NADH concentration.	5.403
$\Delta\Psi_m$	Inner mitochondrial membrane potential.	-140.7
[ISOC]	Isocitrate concentration (mitochondrial).	0.41
[αKG]	α -ketoglutarate concentration (mitochondrial).	2.596×10^{-4}
[SCoA]	Succinyl CoA concentration (mitochondrial).	0.362
[Suc]	Succinate concentration (mitochondrial).	1.06×10^{-3}
[FUM]	Fumarate concentration (mitochondrial).	0.0282
[MAL]	Malate concentration (mitochondrial).	0.01316
[OAA]	Oxalacetate concentration (mitochondrial).	1.623×10^{-6}

REFERENCES

- Balaban, R. S. 2002. Cardiac energy metabolism homeostasis: role of cytosolic calcium. J. Mol. Cell. Cardiol. 34:1259–1271.
- Evans, L., and Y. Matsuoka. 1915. The effect of various mechanical conditions on the gaseous metabolism and efficiency of the mammalian heart. J. Physiol. (Lond.). 49:378–405.
- Brown, G. C. 1992. Control of respiration and ATP synthesis in mammalian mitochondria and cells. *Biochem. J.* 284:1–13.
- Neely, J. R., H. Liebermeister, E. J. Battersby, and H. E. Morgan. 1967. Effect of pressure development on oxygen consumption by isolated rat heart. Am. J. Physiol. 212:804

 –814.
- Williamson, J. R., C. Ford, J. Illingworth, and B. Safer. 1976. Coordination of citric acid cycle activity with electron transport flux. Circ. Res. 38:139–151.
- Heineman, F. W., and R. S. Balaban. 1990. Control of mitochondrial respiration in the heart in vivo. *Annu. Rev. Physiol.* 52:523–542.
- Saks, V. A., A. V. Kuznetsov, M. Vendelin, K. Guerrero, L. Kay, and E. K. Seppet. 2004. Functional coupling as a basic mechanism of feedback regulation of cardiac energy metabolism. *Mol. Cell. Biochem.* 256–257:185–199.
- 8. Chance, B., and G. R. Williams. 1955. A method for the localization of sites for oxidative phosphorylation. *Nature*. 176:250–254.
- Saks, V. A., T. Kaambre, P. Sikk, M. Eimre, E. Orlova, K. Paju, A. Piirsoo, F. Appaix, L. Kay, V. Regitz-Zagrosek, E. Fleck, and E. Seppet. 2001. Intracellular energetic units in red muscle cells. *Biochem. J.* 356:643–657.
- Kaasik, A., V. Veksler, E. Boehm, M. Novotova, A. Minajeva, and R. Ventura-Clapier. 2001. Energetic crosstalk between organelles: architectural integration of energy production and utilization. Circ. Res. 89:153–159.
- Joubert, F., P. Mateo, B. Gillet, J. C. Beloeil, J. L. Mazet, and J. A. Hoerter. 2004. CK flux or direct ATP transfer: versatility of energy transfer pathways evidenced by NMR in the perfused heart. *Mol. Cell. Biochem.* 256–257:43–58.
- Territo, P. R., S. A. French, M. C. Dunleavy, F. J. Evans, and R. S. Balaban. 2001. Calcium activation of heart mitochondrial oxidative phosphorylation: rapid kinetics of mVO₂, NADH, and light scattering. *J. Biol. Chem.* 276:2586–2599.
- Bose, S., S. French, F. J. Evans, F. Joubert, and R. S. Balaban. 2003. Metabolic network control of oxidative phosphorylation: multiple roles of inorganic phosphate. *J. Biol. Chem.* 278:39155–39165.

 Jafri, M. S., J. J. Rice, and R. L. Winslow. 1998. Cardiac Ca²⁺ dynamics: the roles of ryanodine receptor adaptation and sarcoplasmic reticulum load. *Biophys. J.* 74:1149–1168.

- Rice, J. J., M. S. Jafri, and R. L. Winslow. 2000. Modeling short-term interval-force relations in cardiac muscle. *Am. J. Physiol. Heart Circ. Physiol.* 278:H913–H931.
- Cortassa, S., M. A. Aon, E. Marban, R. L. Winslow, and B. O'Rourke. 2003. An integrated model of cardiac mitochondrial energy metabolism and calcium dynamics. *Biophys. J.* 84:2734–2755.
- Brandes, R., and D. M. Bers. 2002. Simultaneous measurements of mitochondrial NADH and Ca²⁺ during increased work in intact rat heart trabeculae. *Biophys. J.* 83:587–604.
- Hoerter, J. A., R. Ventura-Clapier, and A. Kuznetsov. 1994. Compartmentation of creatine kinases during perinatal development of mammalian heart. *Mol. Cell. Biochem.* 133–134:277–286.
- Saks, V. A., R. Ventura-Clapier, and M. K. Aliev. 1996. Metabolic control and metabolic capacity: two aspects of creatine kinase functioning in the cells. *Biochim. Biophys. Acta.* 1274:81–88.
- Shannon, T. R., K. S. Ginsburg, and D. M. Bers. 2000. Reverse mode of the sarcoplasmic reticulum calcium pump and load-dependent cytosolic calcium decline in voltage-clamped cardiac ventricular myocytes. *Biophys. J.* 78:322–333.
- Sakamoto, J., and Y. Tonomura. 1980. Order of release of ADP and Pi from phosphoenzyme with bound ADP of Ca²⁺-dependent ATPase from sarcoplasmic reticulum and of Na⁺, K⁺-dependent ATPase studied by ADP-inhibition patterns. *J. Biochem. (Tokyo)*. 87:1721–1727.
- Jeneson, J. A., H. V. Westerhoff, and M. J. Kushmerick. 2000. A metabolic control analysis of kinetic controls in ATP free energy metabolism in contracting skeletal muscle. Am. J. Physiol. Cell Physiol. 279:C813–C832.
- Regnier, M., D. A. Martyn, and P. B. Chase. 1998. Calcium regulation of tension redevelopment kinetics with 2-deoxy-ATP or low [ATP] in rabbit skeletal muscle. *Biophys. J.* 74:2005–2015.
- Karatzaferi, C., K. H. Myburgh, M. K. Chinn, K. Franks-Skiba, and R. Cooke. 2003. Effect of an ADP analog on isometric force and ATPase activity of active muscle fibers. *Am.J. Physiol. Cell Physiol.* 284:C816–C825.
- Pate, E., and R. Cooke. 1989. A model of crossbridge action: the effects of ATP, ADP and Pi. J. Muscle Res. Cell Motil. 10:181–196.
- Luo, C. H., and Y. Rudy. 1994. A dynamic model of the cardiac ventricular action potential. I. Simulations of ionic currents and concentration changes. Circ. Res. 74:1071–1096.
- Nakao, M., and D. C. Gadsby. 1989. [Na] and [K] dependence of the Na/K pump current-voltage relationship in Guinea-pig ventricular myocytes. J. Gen. Physiol. 94:539–565.
- Echarte, M. M., V. Levi, A. M. Villamil, R. C. Rossi, and J. P. Rossi. 2001. Quantitation of plasma membrane calcium pump phosphorylated intermediates by electrophoresis. *Anal. Biochem.* 289:267–273.
- Pasa, T. C., A. S. Otero, H. Barrabin, and H. M. Scofano. 1992. Regulation of the nucleotide dependence of the cardiac sarcolemma Ca²⁺-ATPase. *J. Mol. Cell. Cardiol*. 24:233–242.
- Ebus, J. P., and G. J. Stienen. 1996. Origin of concurrent ATPase activities in skinned cardiac trabeculae from rat. J. Physiol. 492:675–687.
- 31. Cohen, S. D., and A. C. Hindmarsh. 1994. CVODE User Guide. *In* Lawrence Livermore National Laboratory report. Livermore, CA.
- Brandes, R., and D. M. Bers. 1999. Analysis of the mechanisms of mitochondrial NADH regulation in cardiac trabeculae. *Biophys. J.* 77:1666–1682.
- Mulieri, L. A., G. Hasenfuss, F. Ittleman, E. M. Blanchard, and N. R. Alpert. 1989. Protection of human left ventricular myocardium from cutting injury with 2,3-butanedione monoxime. *Circ. Res.* 65:1441– 1449
- Janssen, P. M., L. B. Stull, and E. Marban. 2002. Myofilament properties comprise the rate-limiting step for cardiac relaxation at body temperature in the rat. Am. J. Physiol. Heart Circ. Physiol. 282:H499–H507.
- Szigligeti, P., C. Pankucsi, T. Banyasz, A. Varro, and P. P. Nanasi.
 1996. Action potential duration and force-frequency relationship in

- isolated rabbit, Guinea-pig and rat cardiac muscle. *J. Comp. Physiol.* [*B*]. 166:150–155.
- Maier, L. S., D. M. Bers, and B. Pieske. 2000. Differences in Ca²⁺-handling and sarcoplasmic reticulum Ca²⁺-content in isolated rat and rabbit myocardium. *J. Mol. Cell. Cardiol.* 32:2249–2258.
- Neely, J. R., M. Whitmer, and S. Mochizuki. 1976. Effects of mechanical activity and hormones on myocardial glucose and fatty acid utilization. *Circ. Res.* 38:122–130.
- Elliott, A. C., G. L. Smith, and D. G. Allen. 1994. The metabolic consequences of an increase in the frequency of stimulation in isolated ferret hearts. *J. Physiol.* 474:147–159.
- Jacobus, W. E. 1985. Respiratory control and the integration of heart high-energy phosphate metabolism by mitochondrial creatine kinase. *Annu. Rev. Physiol.* 47:707–725.
- 40. Chen, C., Y. Ko, M. Delannoy, S. J. Ludtke, W. Chiu, and P. L. Pedersen. 2004. Mitochondrial ATP synthasome: three-dimensional structure by electron microscopy of the ATP synthase in complex formation with carriers for Pi and ADP/ATP. *J. Biol. Chem.* 279: 31761–31768.
- Bers, D. M. 2001. Excitation-Contraction Coupling and Cardiac Contractile Force. Kluwer Academic Publishers, Dordrecht, The Netherlands: Boston, MA.
- Eijgelshoven, M. H., J. H. van Beek, I. Mottet, M. G. Nederhoff, C. J. van Echteld, and N. Westerhof. 1994. Cardiac high-energy phosphates adapt faster than oxygen consumption to changes in heart rate. *Circ. Res.* 75:751–759.
- 43. Harrison, G. J., M. H. van Wijhe, B. de Groot, F. J. Dijk, L. A. Gustafson, and J. H. van Beek. 2003. Glycolytic buffering affects cardiac bioenergetic signaling and contractile reserve similar to creatine kinase. Am. J. Physiol. Heart Circ. Physiol. 285:H883–H890.
- Brandes, R., and D. M. Bers. 1997. Intracellular Ca²⁺ increases the mitochondrial NADH concentration during elevated work in intact cardiac muscle. Circ. Res. 80:82–87.
- 45. Kadenbach, B. 2003. Intrinsic and extrinsic uncoupling of oxidative phosphorylation. *Biochim. Biophys. Acta.* 1604:77–94.
- Bittl, J. A., and J. S. Ingwall. 1985. Reaction rates of creatine kinase and ATP synthesis in the isolated rat heart. A ³¹P NMR magnetization transfer study. *J. Biol. Chem.* 260:3512–3517.
- Johnson, E. A. 1979. Force-interval relationship in cardiac muscle. *In* Handbook of Physiology. The Cardiovascular System. The Heart. American Physiological Society, Bethesda, MD. 475–492.
- Wier, W. G., and D. T. Yue. 1986. Intracellular calcium transients underlying the short-term force-interval relationship in ferret ventricular myocardium. *J. Physiol.* 376:507–530.
- Huser, J., L. A. Blatter, and S. S. Sheu. 2000. Mitochondrial calcium in heart cells: beat-to-beat oscillations or slow integration of cytosolic transients? *J. Bioenerg. Biomembr.* 32:27–33.
- 50. Maack, C., S. Cortassa, M. A. Aon, A. N. Ganesan, T. Liu, and B. O'Rourke. 2006. Elevated cytosolic Na⁺ decreases mitochondrial Ca²⁺ uptake during excitation-contraction coupling and impairs energetic adaptation in cardiac myocytes. *Circ. Res.* In press.
- Pozzan, T., and R. Rizzuto. 2000. The renaissance of mitochondrial calcium transport. Eur. J. Biochem. 267:5269–5273.
- Magnus, G., and J. Keizer. 1998. Model of β-cell mitochondrial calcium handling and electrical activity. I. Cytoplasmic variables. Am. J. Physiol. 274:C1158–C1173.
- Matsuoka, S., N. Sarai, H. Jo, and A. Noma. 2004. Simulation of ATP metabolism in cardiac excitation-contraction coupling. *Prog. Biophys. Mol. Biol.* 85:279–299.
- Korzeniewski, B., and J. P. Mazat. 1996. Theoretical studies on the control of oxidative phosphorylation in muscle mitochondria: application to mitochondrial deficiencies. *Biochem. J.* 319:143–148.
- Vendelin, M., O. Kongas, and V. Saks. 2000. Regulation of mitochondrial respiration in heart cells analyzed by reaction-diffusion model of energy transfer. Am. J. Physiol. Cell Physiol. 278:C747– C764.

- Vendelin, M., M. Lemba, and V. A. Saks. 2004. Analysis of functional coupling: mitochondrial creatine kinase and adenine nucleotide translocase. *Biophys. J.* 87:696–713.
- Page, E. 1978. Quantitative ultrastructural analysis in cardiac membrane physiology. Am. J. Physiol. 235:C147–C158.
- Sheu, S. S., and H. A. Fozzard. 1982. Transmembrane Na⁺ and Ca²⁺ electrochemical gradients in cardiac muscle and their relationship to force development. *J. Gen. Physiol.* 80:325–351.
- Sheu, S. S. 1989. Cytosolic sodium concentration regulates contractility of cardiac muscle. *Basic Res. Cardiol.* 84(Suppl 1):35–45.
- Elimban, V., D. Zhao, and N. S. Dhalla. 1987. A comparative study of the rat heart sarcolemmal Ca²⁺-dependent ATPase and myosin ATPase. *Mol. Cell. Biochem.* 77:143–152.
- Winslow, R. L., J. Rice, S. Jafri, E. Marban, and B. O'Rourke. 1999.
 Mechanisms of altered excitation-contraction coupling in canine tachycardia-induced heart failure, II: model studies. *Circ. Res.* 84:571–586
- Ruf, T., S. Hebisch, R. Gross, N. Alpert, H. Just, and C. Holubarsch. 1996. Modulation of myocardial economy and efficiency in mammalian failing and non-failing myocardium by calcium channel activation and β-adrenergic stimulation. *Cardiovasc. Res.* 32:1047–1055.
- 63. Selivanov, V. A., A. E. Alekseev, D. M. Hodgson, P. P. Dzeja, and A. Terzic. 2004. Nucleotide-gated KATP channels integrated with creatine and adenylate kinases: amplification, tuning and sensing of energetic signals in the compartmentalized cellular environment. *Mol. Cell. Biochem.* 256–257:243–256.

- 64. Joubert, F., B. Gillet, J. L. Mazet, P. Mateo, J. Beloeil, and J. A. Hoerter. 2000. Evidence for myocardial ATP compartmentation from NMR inversion transfer analysis of creatine kinase fluxes. *Biophys. J.* 79:1–13.
- Ingwall, J. S., and R. G. Weiss. 2004. Is the failing heart energystarved? On using chemical energy to support cardiac function. *Circ. Res.* 95:135–145.
- 66. Saupe, K. W., M. Spindler, J. C. Hopkins, W. Shen, and J. S. Ingwall. 2000. Kinetic, thermodynamic, and developmental consequences of deleting creatine kinase isoenzymes from the heart. Reaction kinetics of the creatine kinase isoenzymes in the intact heart. *J. Biol. Chem.* 275:19742–19746.
- Clark, J. F., A. V. Kuznetsov, and G. K. Radda. 1997. ADPregenerating enzyme systems in mitochondria of guinea pig myometrium and heart. *Am. J. Physiol.* 272:C399–C404.
- 68. Rutter, G. A., and R. M. Denton. 1988. Regulation of NAD⁺-linked isocitrate dehydrogenase and 2-oxoglutarate dehydrogenase by Ca²⁺ ions within toluene-permeabilized rat heart mitochondria. Interactions with regulation by adenine nucleotides and NADH/NAD⁺ ratios. *Biochem. J.* 252:181–189.
- Randle, P. J., and P. K. Tubbs. 1979. Carbohydrate and fatty acid metabolism. *In Handbook of Physiology*. R. M. Berne, N. Sperelakis, and R. Geiger, editors. American Physiological Society, Bethesda, MD. 805–844.
- Gunter, K. K., and T. E. Gunter. 1994. Transport of calcium by mitochondria. J. Bioenerg. Biomembr. 26:471

 –485.
- Gunter, T. E., and D. R. Pfeiffer. 1990. Mechanisms by which mitochondria transport calcium. Am. J. Physiol. 258:C755–C786.